

# **(Non-)reciprocity and nanotechnology: demonstration of a nonlinear optical diode**

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**EPFL**



DOUBLE WORD

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S<sub>1</sub>

C<sub>3</sub>

R<sub>1</sub>

A<sub>1</sub>

B<sub>3</sub>

B<sub>3</sub>

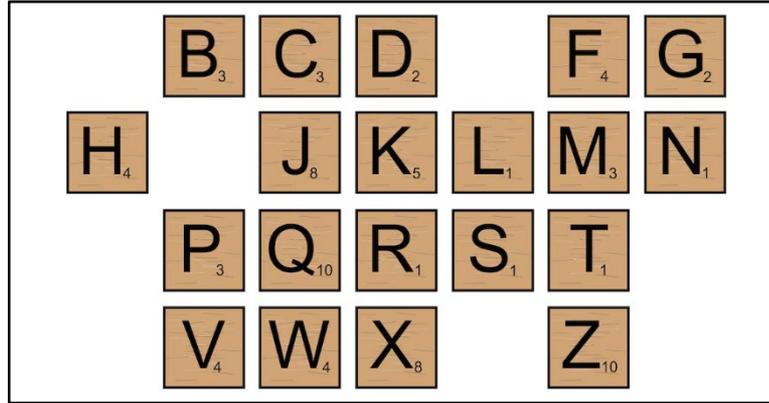
L<sub>1</sub>

E<sub>1</sub>

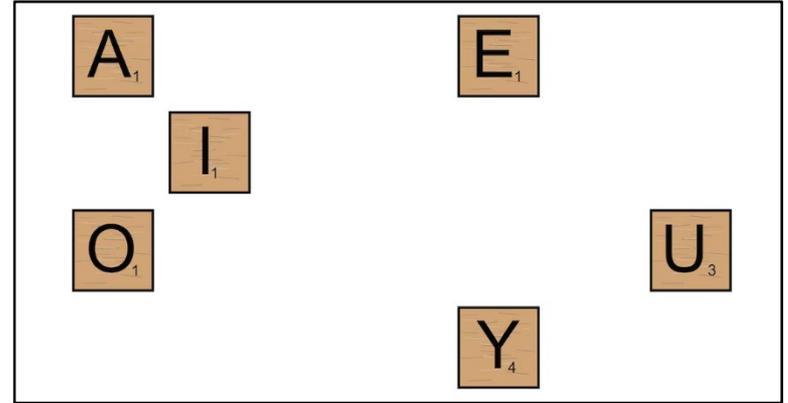
# Using the entire alphabet

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Set 1

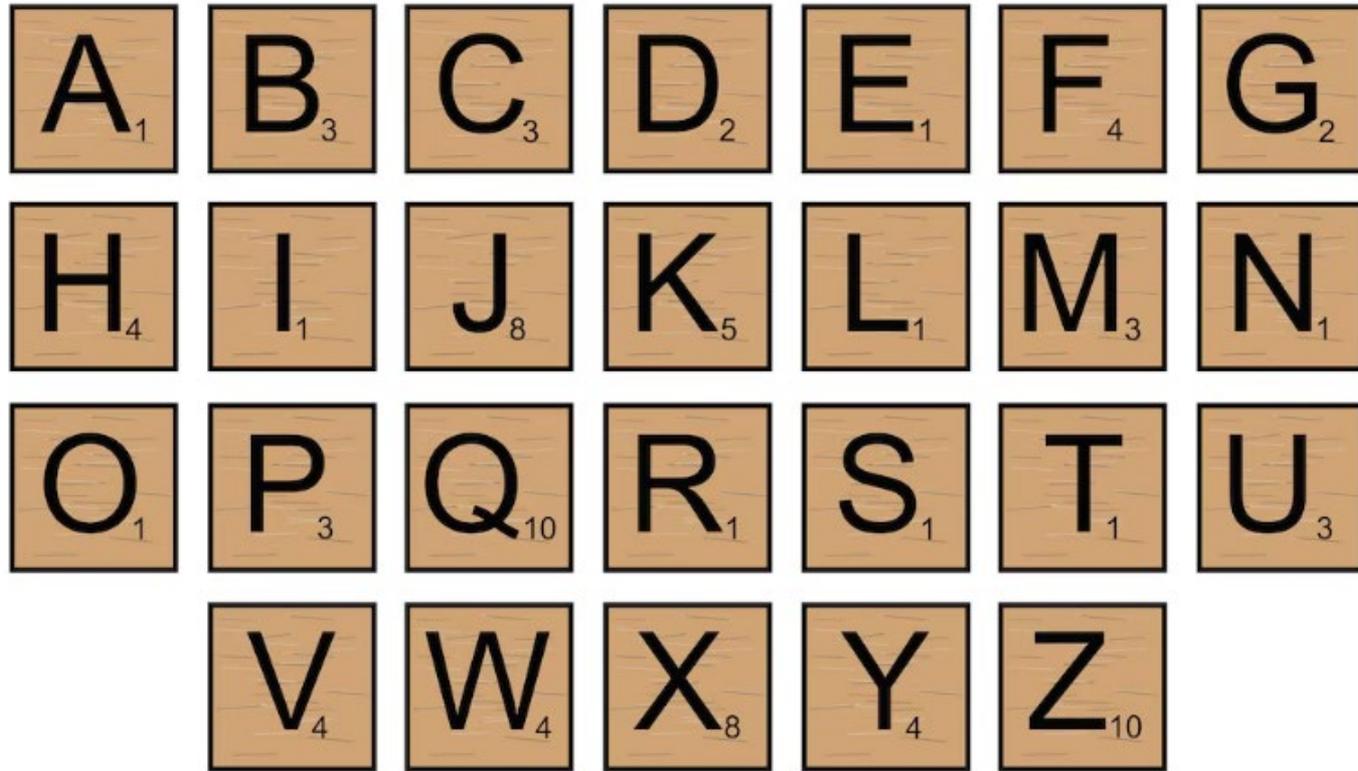


Set 2



# Using the entire alphabet

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# Using the entire electromagnetic alphabet

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$$\nabla \times \mathbf{E}(\mathbf{r}, t) = -\frac{\partial \mathbf{B}(\mathbf{r}, t)}{\partial t}$$

$$\nabla \times \mathbf{H}(\mathbf{r}, t) = \frac{\partial \mathbf{D}(\mathbf{r}, t)}{\partial t} + \mathbf{J}(\mathbf{r}, t)$$

$$\nabla \cdot \mathbf{D}(\mathbf{r}, t) = \rho(\mathbf{r}, t)$$

$$\nabla \cdot \mathbf{B}(\mathbf{r}, t) = 0$$

$$\begin{pmatrix} \mathbf{p} \\ \mathbf{m} \end{pmatrix} = \begin{pmatrix} \underline{\underline{\alpha}}_{ee} & \underline{\underline{\alpha}}_{em} \\ \underline{\underline{\alpha}}_{me} & \underline{\underline{\alpha}}_{mm} \end{pmatrix} \cdot \begin{pmatrix} \mathbf{E} \\ \mathbf{H} \end{pmatrix}$$

magneto-electric  
coupling terms  
(bianisotropy)

# Using the entire electromagnetic alphabet

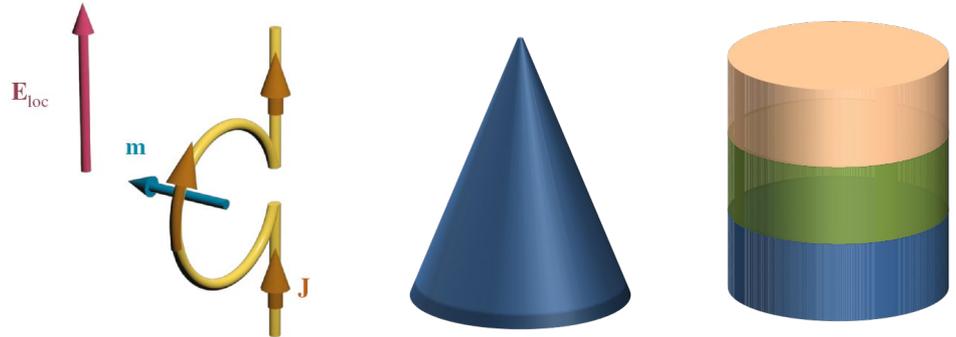
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- Strong bianisotropy requires breaking the symmetry of the system...
- ... including in the out-of-plane direction...
- ... which is very challenging for nanotechnology !
- It can also be achieved by using simple shapes built from different materials!

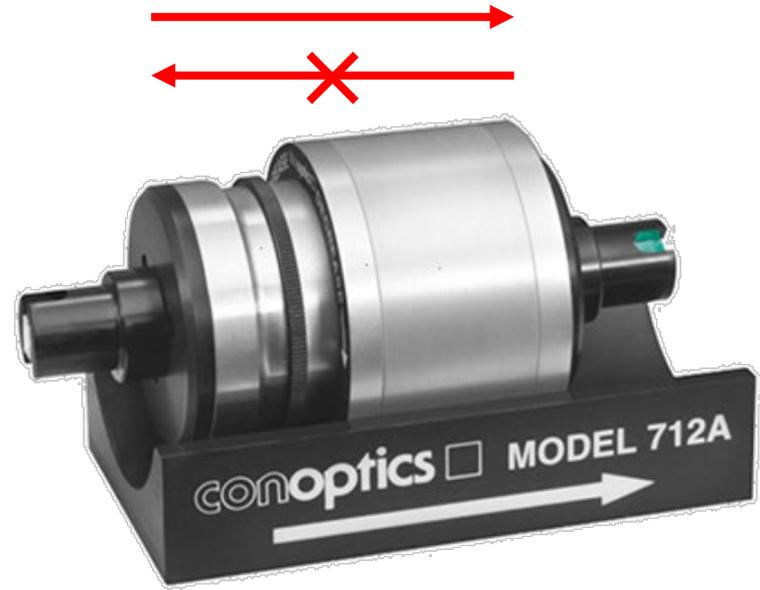
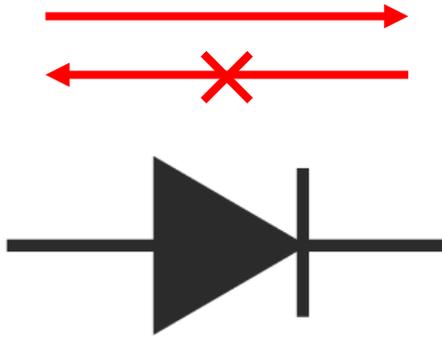
# Outline

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- Introduction
- Nonreciprocal devices
- Second harmonic generation in plasmonic systems
- Putting numerical techniques to good use
- Nanotechnologies
- Nonlinear optical diode
- Is it non-reciprocal?
- Summary

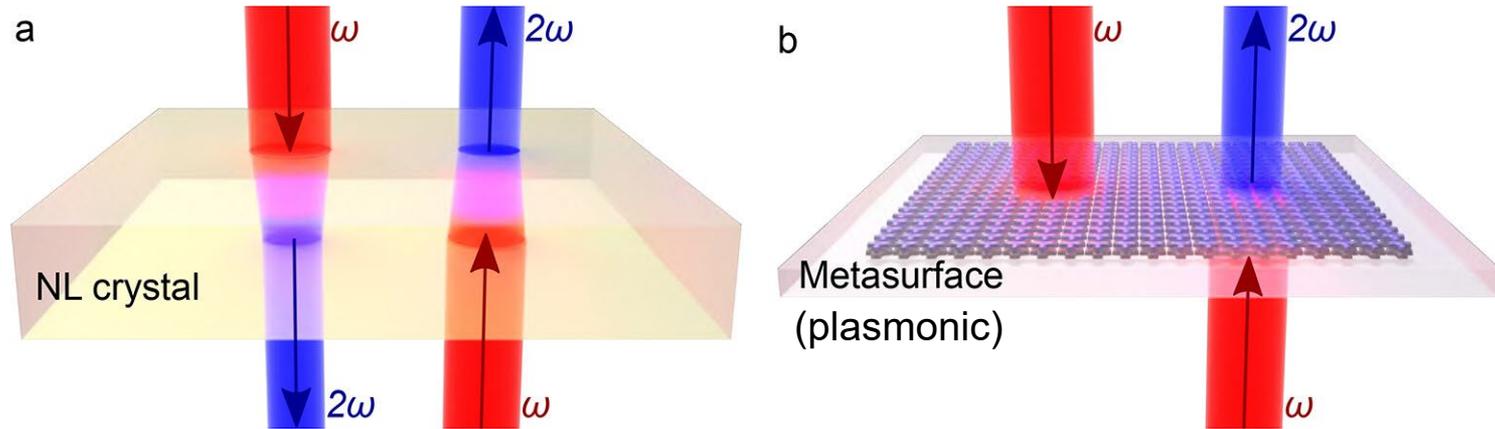
# Nonreciprocal devices

- Allow the signal to pass only in one direction
- Are key for signal processing
- In optics, require an external time-odd bias, such as a magnetic field

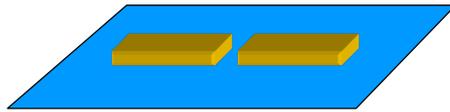


# Asymmetric second harmonic generation (SHG)

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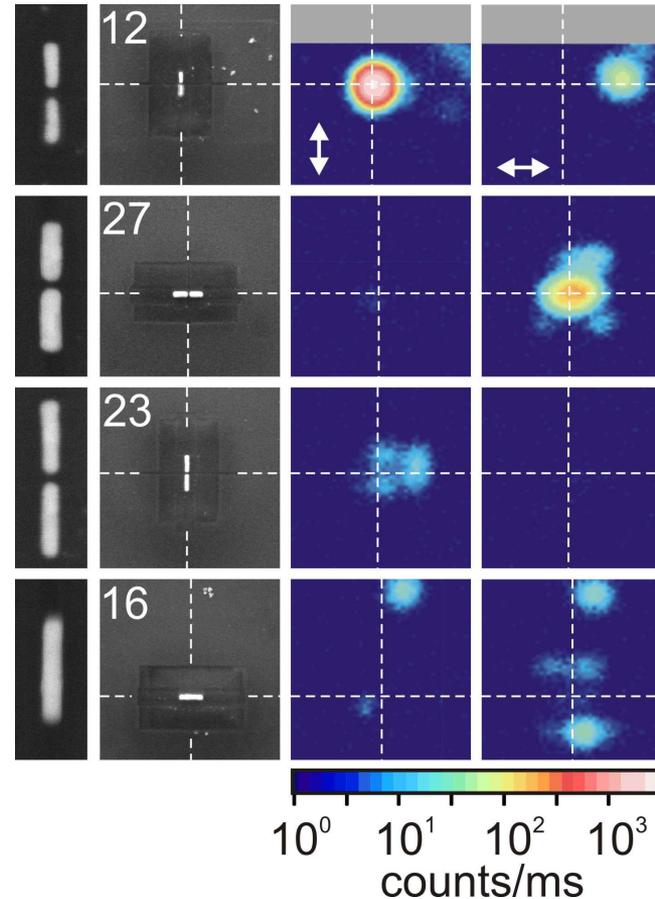


# Plasmonic dipole antenna

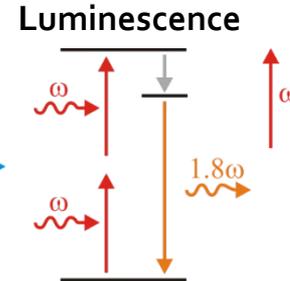
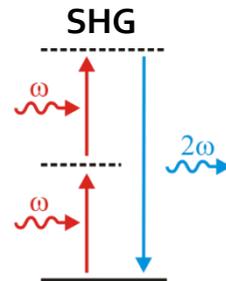
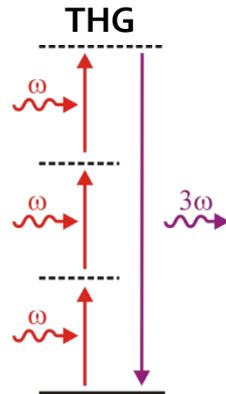
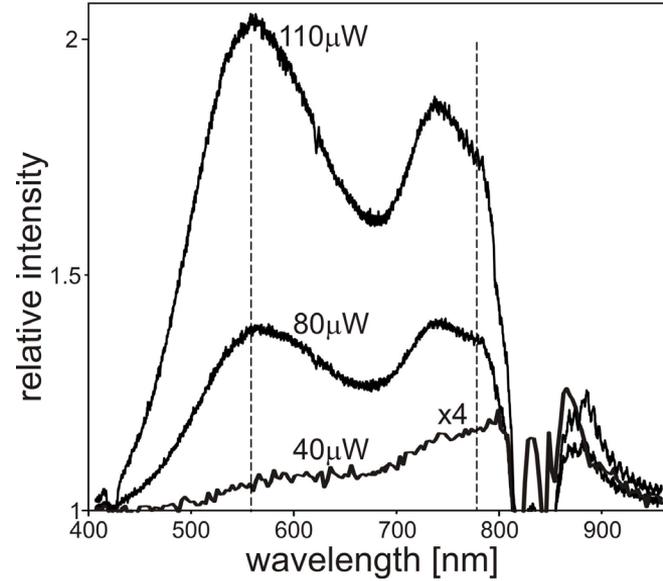
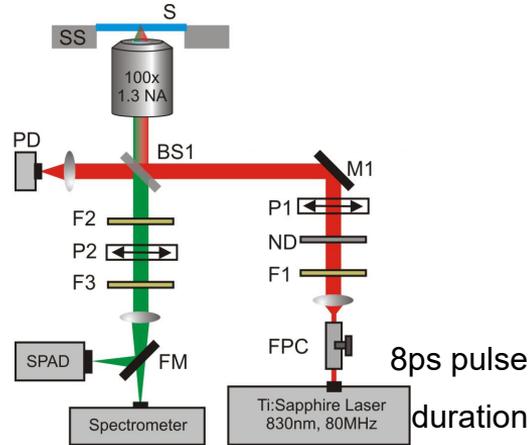


Focused ion beam fabrication:

- 40nm thick gold
- Length: 190...400nm
- Width: 45nm
- Gap: 20nm
- Glass substrate



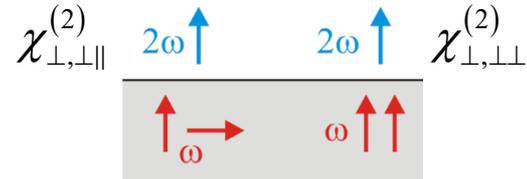
# Plasmonic dipole antenna – Nonlinear effects



## Second order susceptibility tensor

$$P_\alpha(2\omega) = \varepsilon_0 \chi_{\alpha,\beta\gamma}^{(2)} E_\beta(\omega) E_\gamma(\omega)$$

- In the bulk:  $\alpha, \beta, \gamma = x, y$  or  $z$
- At an interface:  $\alpha, \beta, \gamma = \parallel$  or  $\perp$



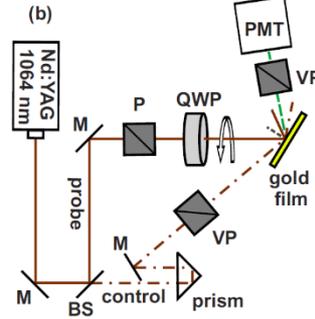
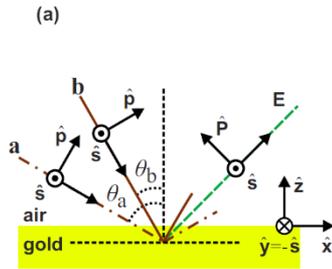
- For plasmonic metals, the  $\chi_{\perp,\perp\perp}^{(2)}$  component dominates
- Classical SHG requires phase matching between the waves at  $\omega$  and  $2\omega$  that travel together, which is complicated and requires an anisotropic crystal and control of polarization:

The diagram shows two parallel waves traveling to the right. The upper wave is blue and the lower wave is red. The equation  $P_\alpha(2\omega) = \chi_{\alpha,\beta\beta}^{(2)} E_\beta(\omega) E_\beta(\omega)$  is shown to the right of the waves.

- This is (generally) not the case for SHG in plasmonic nanostructures (“zero phase matching”)

# SHG: Surface vs bulk contributions

- Measurement of bulk and surface contributions:

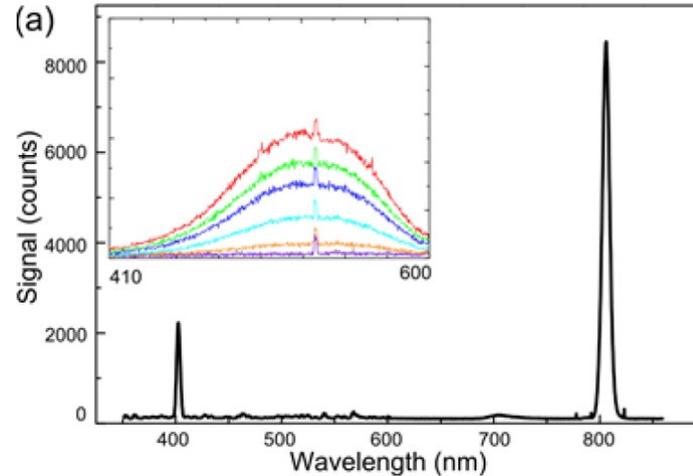
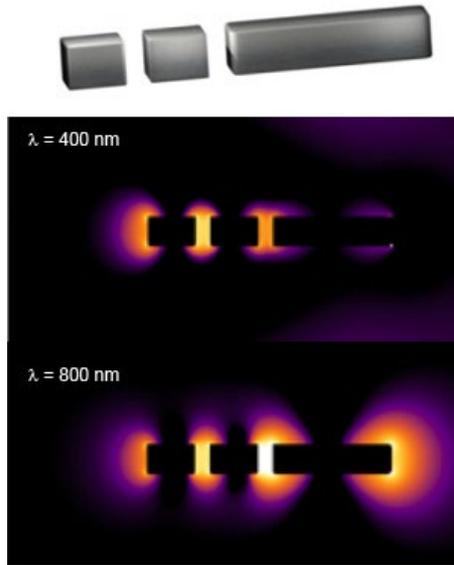


Contribution to the measured SH signals				Character
$f_{ppp}$	$f_{pss}$	$f_{sps}$	$f_{sss}$	
1.3				Surface and bulk
1.5	1.0			Surface and bulk
3.5		2.2	0.6	Surface only
0.004		0.2	0.1	Bulk only

- For plasmonic metals the surface contributions dominate over the bulk; there are however specific experimental conditions, where  $\chi_{\text{bulk}}^{(2)}$  cannot be neglected

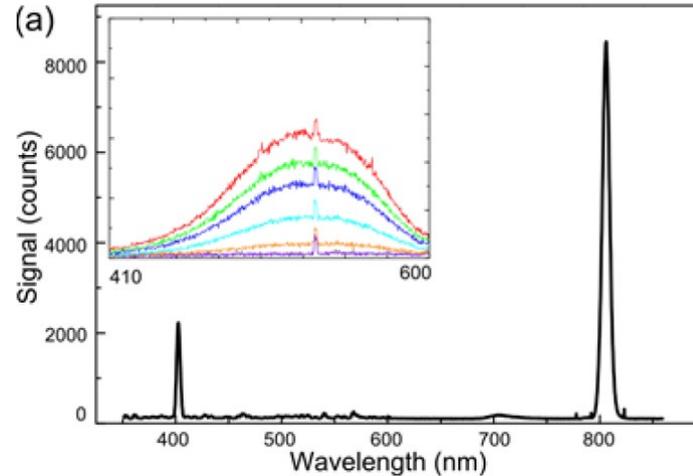
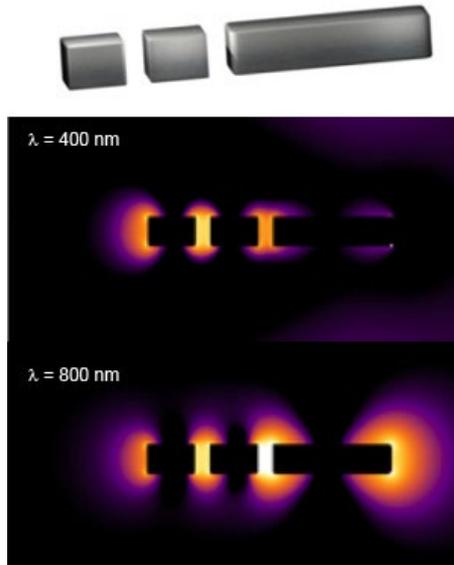
# Double resonant antenna and second harmonic generation

- A plasmonic nanostructure with two resonances: at the fundamental and at the second harmonic frequency



# Double resonant antenna and second harmonic generation

- How does SHG work in such a structure?
- What is the role of the different parts in the antenna?



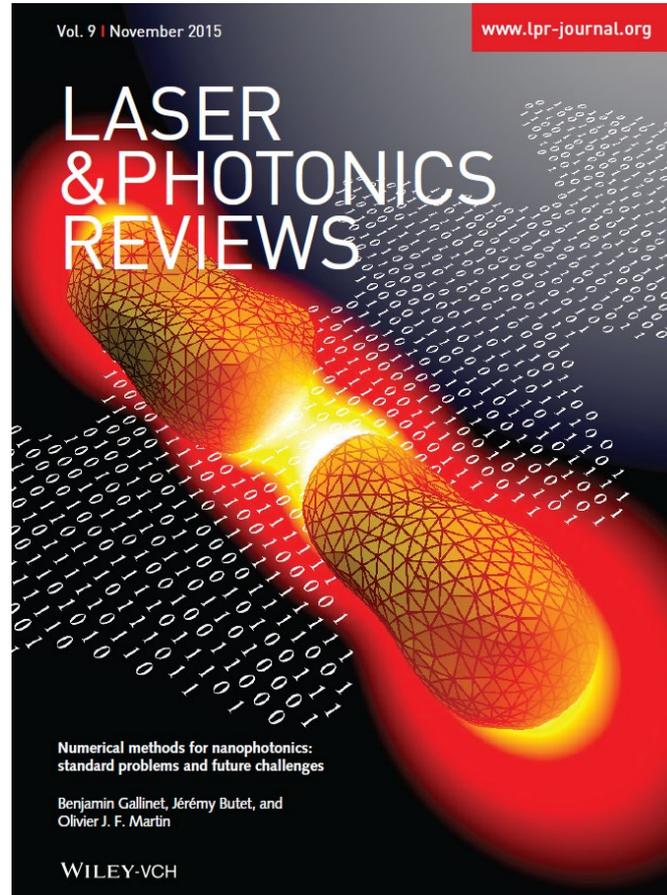
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# Review on numerical methods for nanophotonics/plasmonics

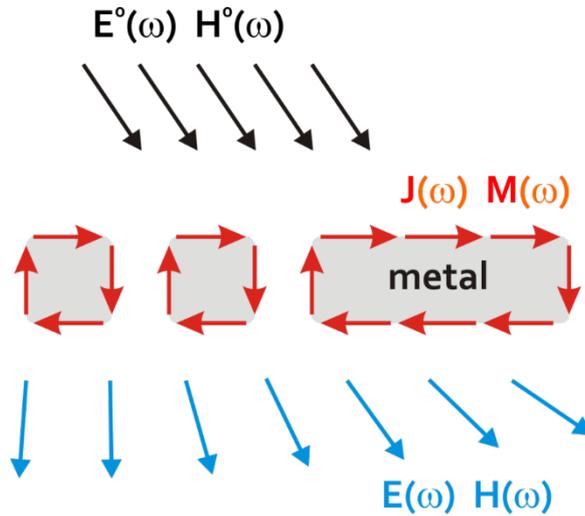
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**B. Gallinet, J. Butet, and O.J.F. Martin**  
**Laser & Photonics Reviews vol. 9,**  
**p. 577 (2015)**

# Surface integral equation (SIE) method – Linear regime

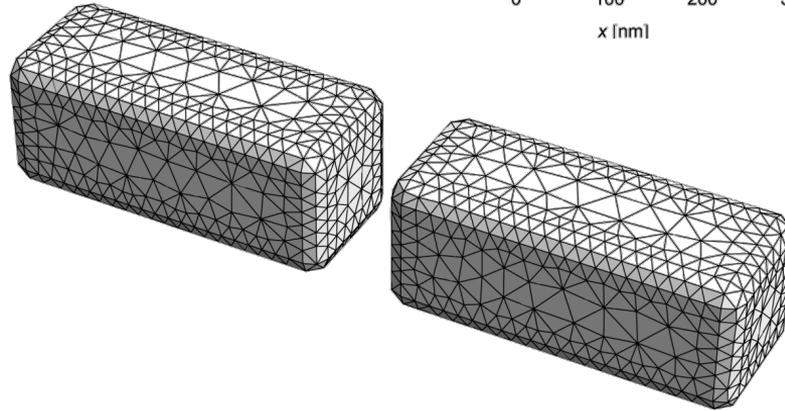
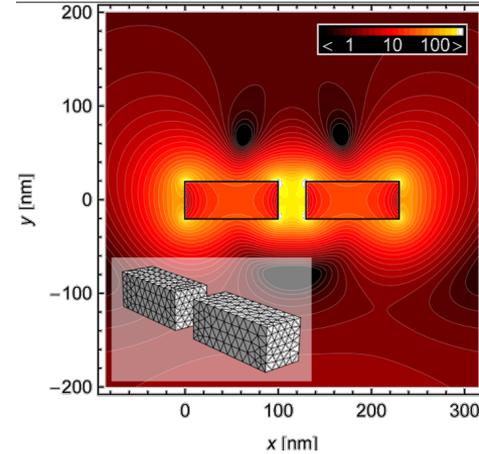
- Light scattered is computed by means of surface currents on the scatterers



# Modelling plasmonic structures accurately

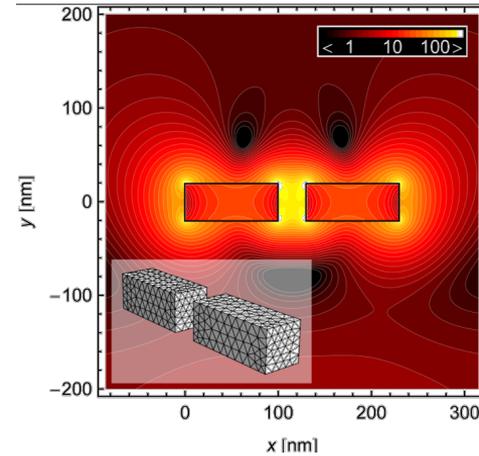
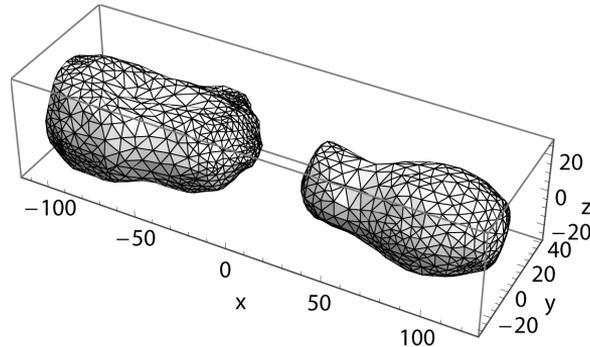
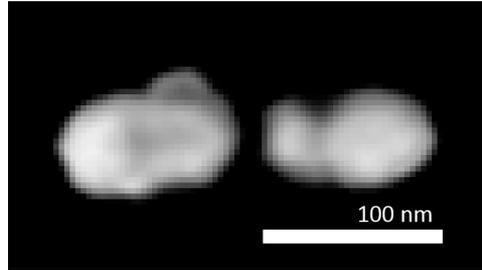
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- Finite elements
- surface integral formulation:
  - Fast
  - Versatile
  - Very accurate
  - Useful for comparison with experiments



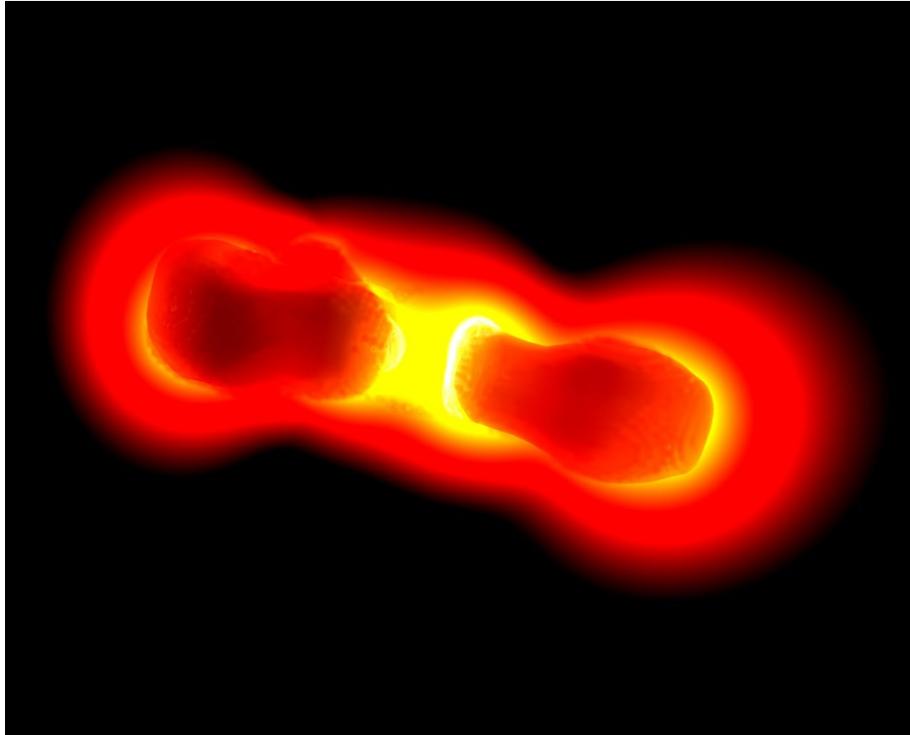
# Modelling realistic nanostructures

- Sometimes the nanofabrication is not so perfect...

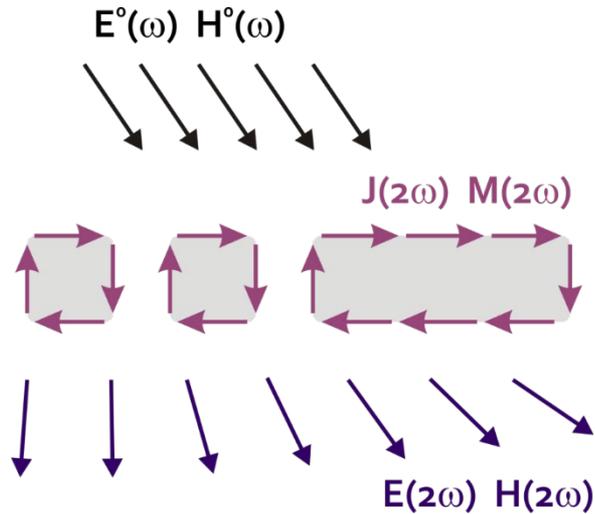


# Modelling realistic nanostructures

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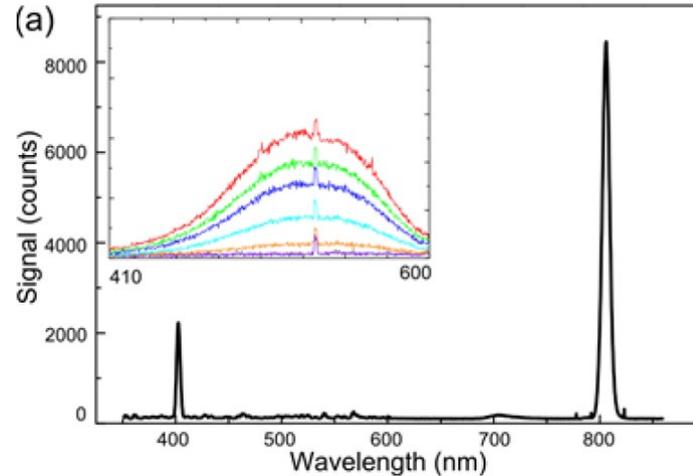
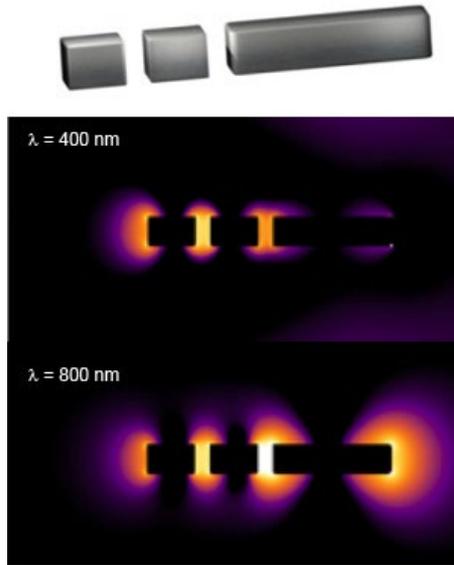
## Surface integral equation (SIE) method – Computing SHG



- Compute electric and magnetic surface currents at  $\omega$
- For each mesh, compute the normal field component at  $\omega$  inside the metal
- Use  $P_n(2\omega) = \chi_{n,nn}^{(2)} E_n(\omega) E_n(\omega)$  to obtain the surface currents at  $2\omega$
- Solve again the scattering problem with those currents to get the fields at  $2\omega$

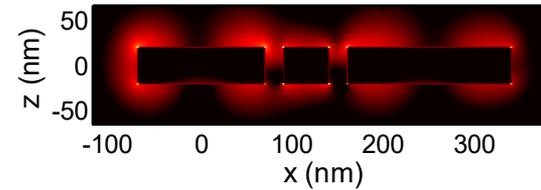
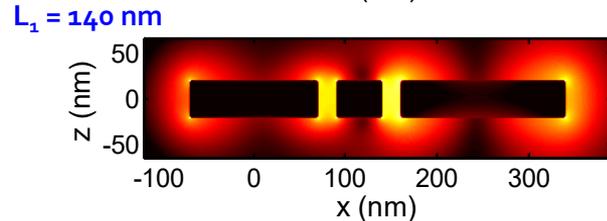
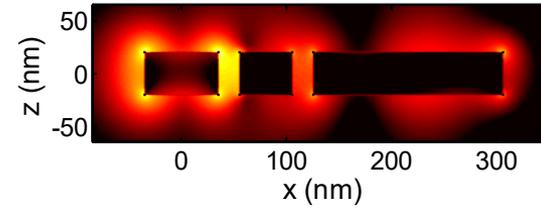
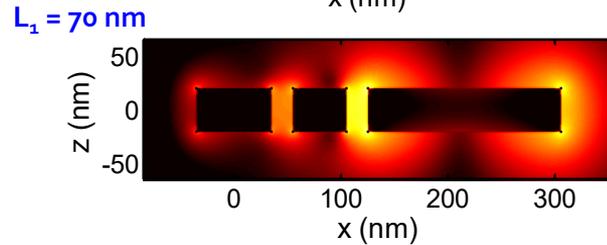
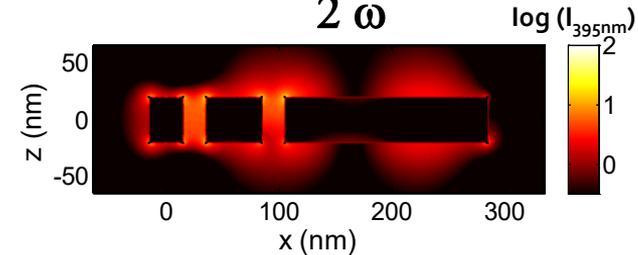
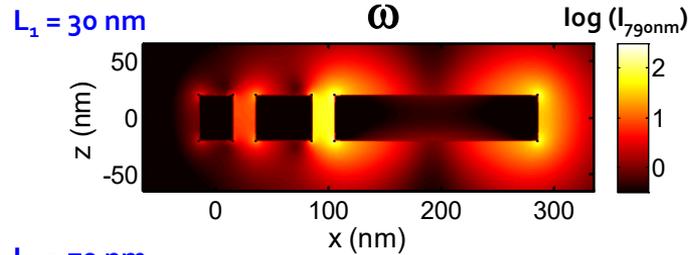
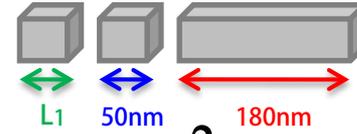
# Double resonant antenna and second harmonic generation

- How does SHG work in such a structure?
- What is the role of the different parts in the antenna?



# Elucidating the role of the different parts of the antenna

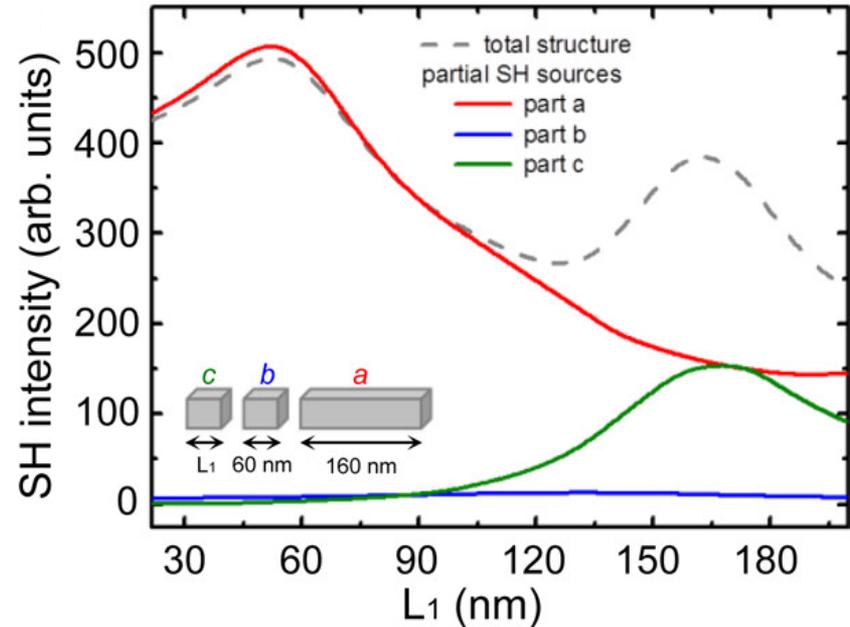
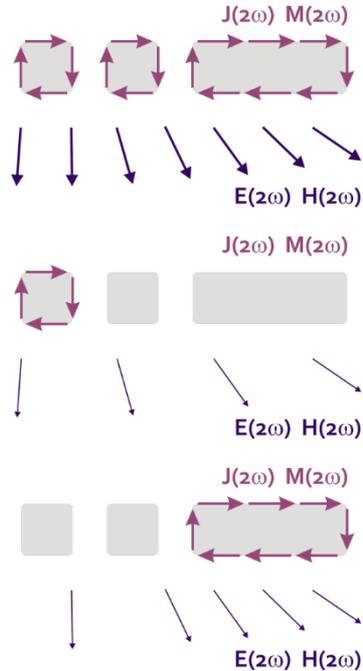
- Tuning one of the short bars



- It looks like the short bar determines the SHG emission

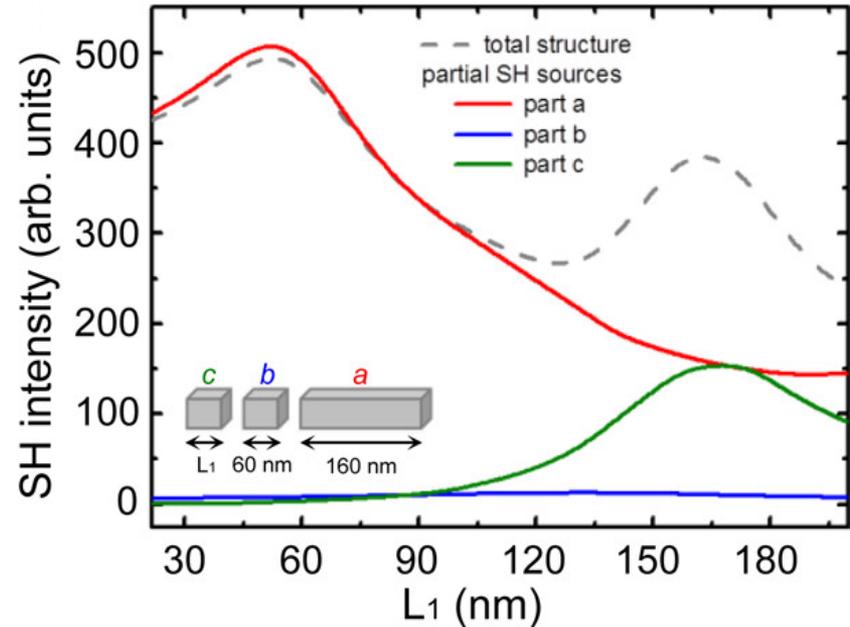
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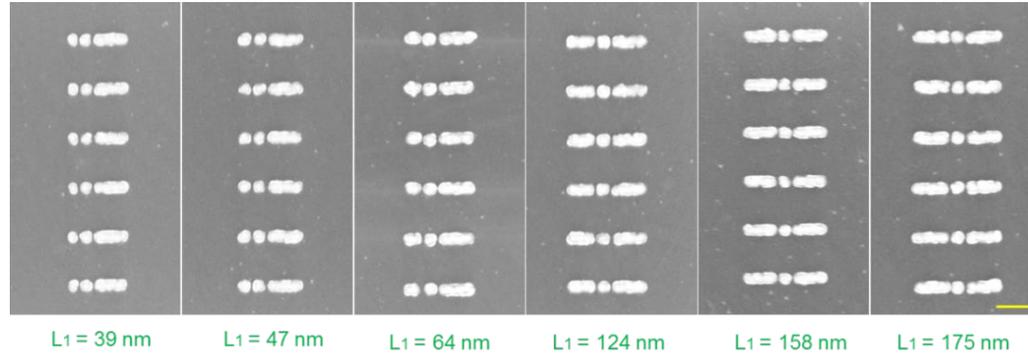


## Elucidating the role of the different parts of the antenna

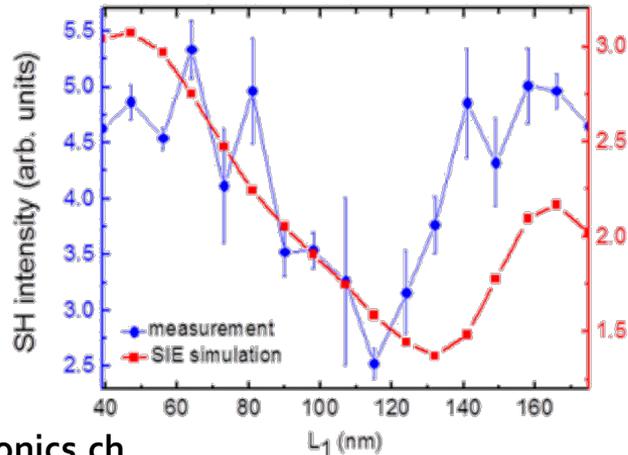
- It looks like the short bar determines the SHG emission...
- ... but things are more complicated!
  - The small bar tunes the structure
  - SHG comes from the large bar



# Elucidating the role of the different parts of the antenna



$L_1 = 39, 47, 56, 64, 73, 81, 90, 98, 107, 115, 124, 132, 141, 149, 158, 166, 175$  nm



- Good agreement between measurements and simulations

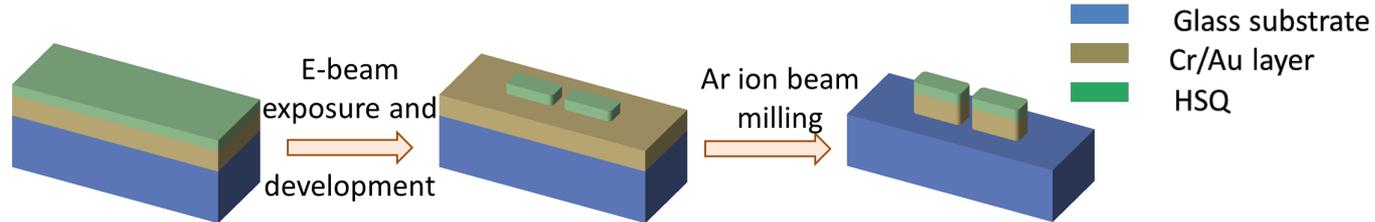
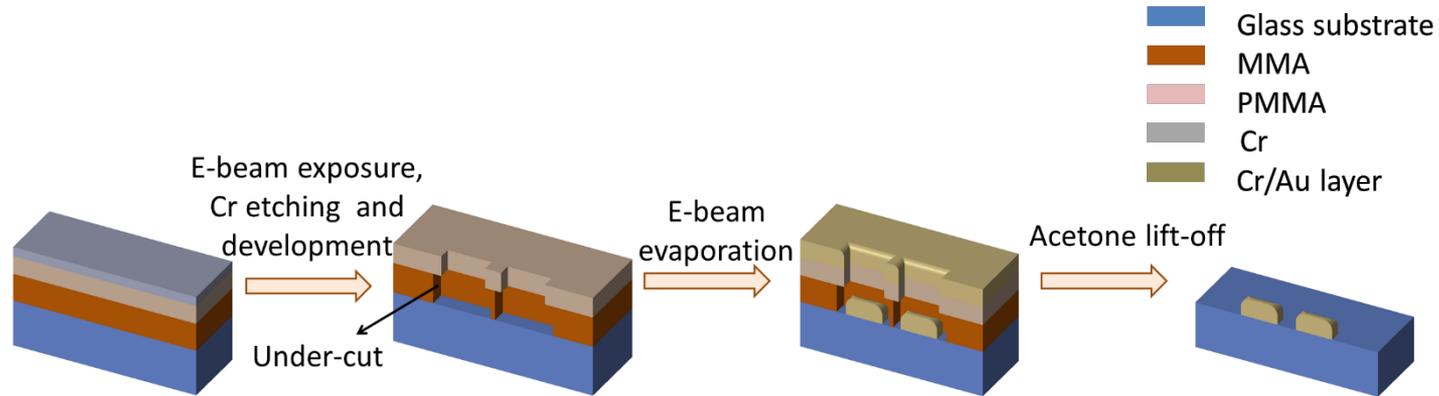
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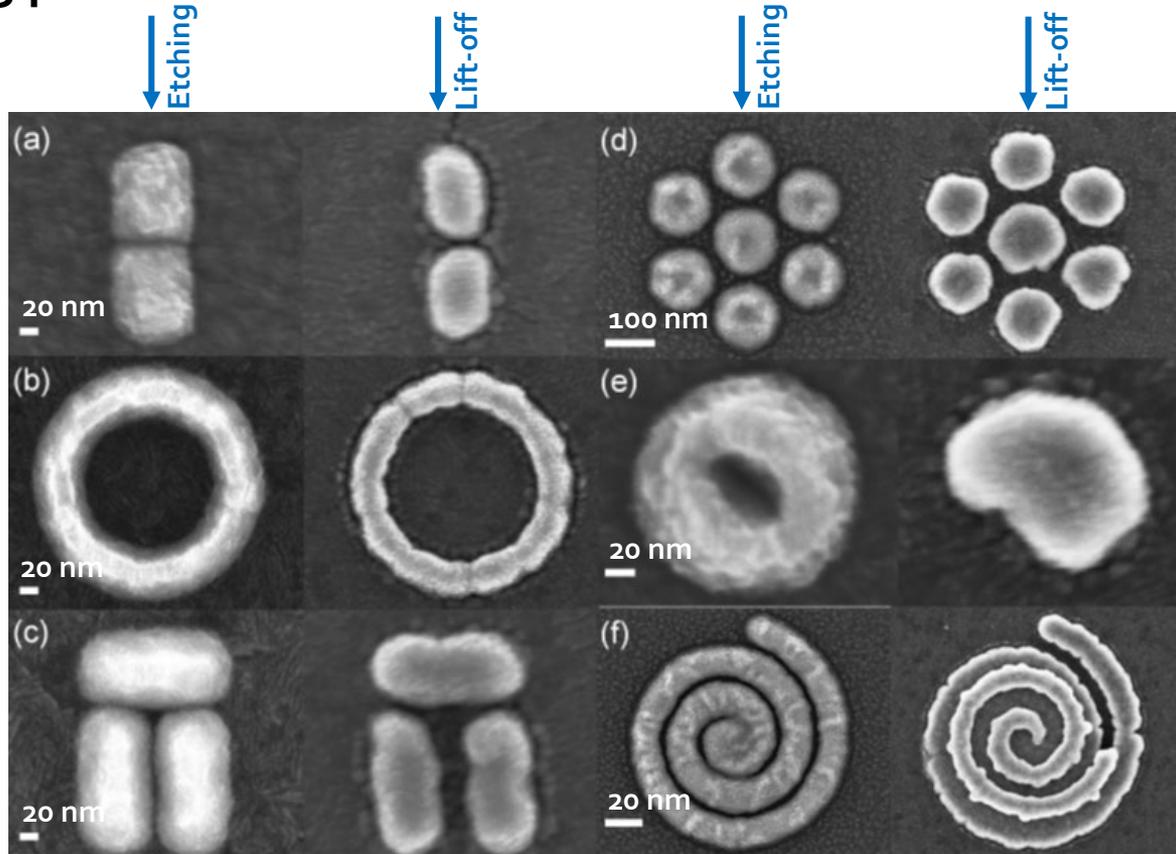
# Nanofabrication of plasmonic structures

- Lift-off (positive resist) vs. ion etching (negative resist)



# Lift-off vs. ion etching (gold nanostructures)

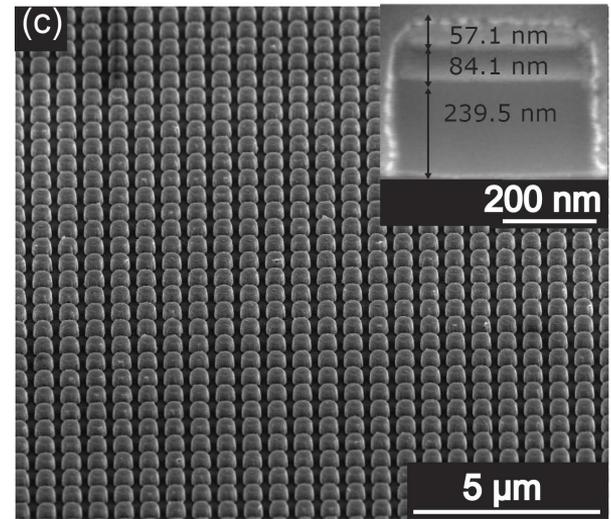
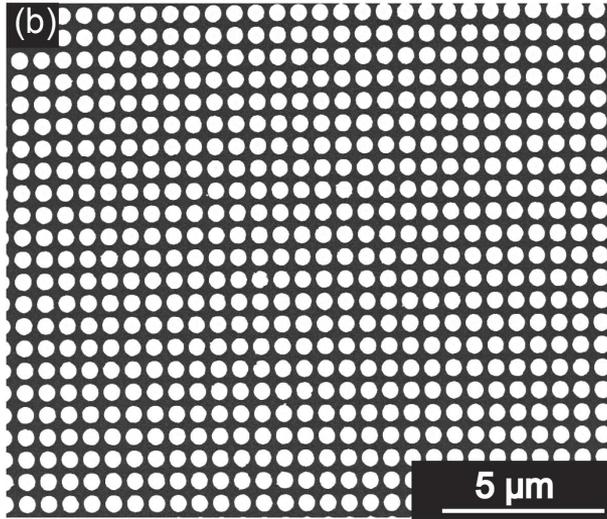
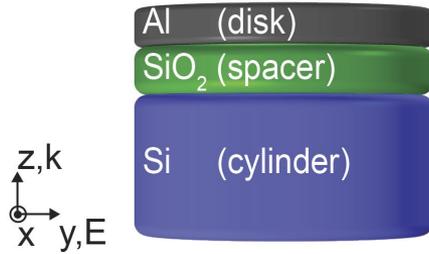
- Ion etching provides smaller features and better control



# Hybrid metasurface for sensing

- Etching can fabricate quite thick nanostructures

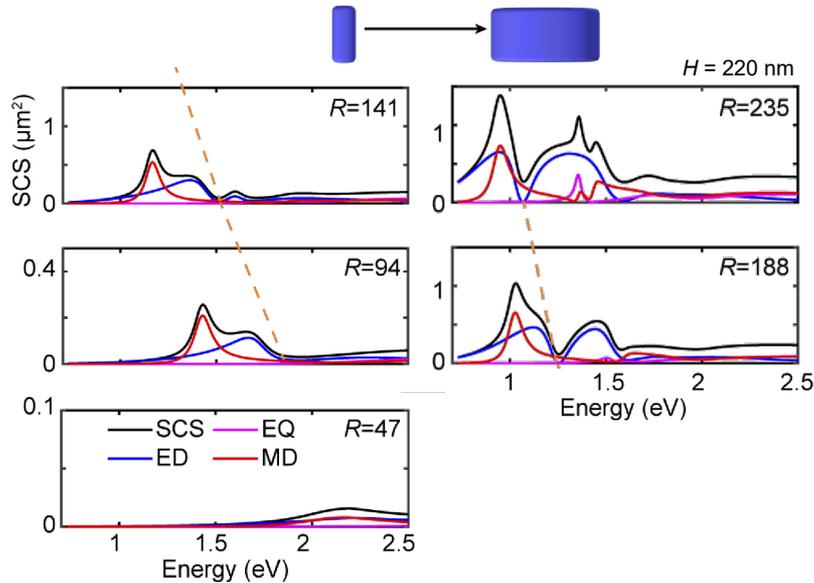
(a)



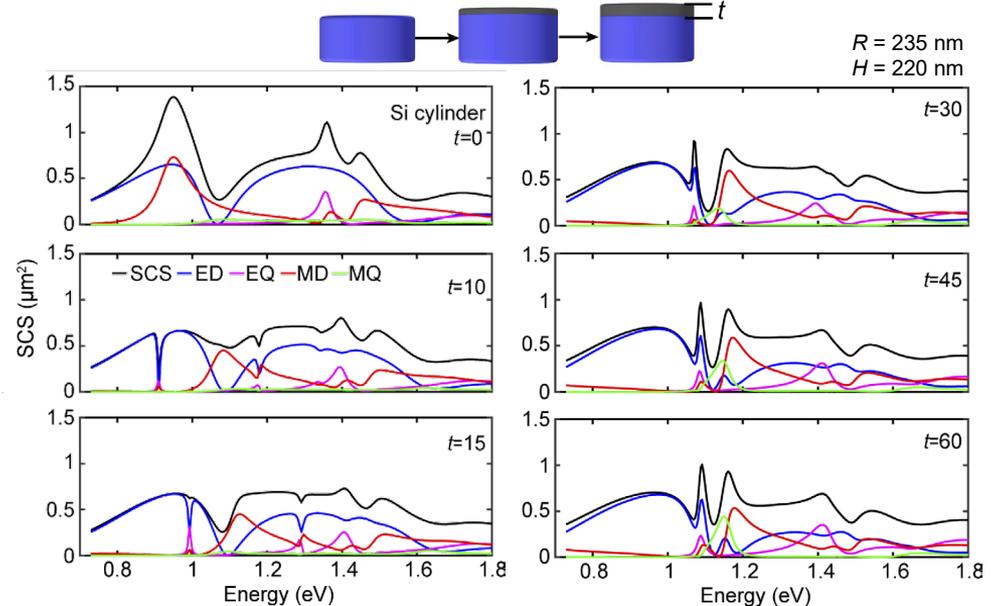
# Hybrid nanostructures – Many degrees of freedom to tune the response

- Dielectric structures support a magnetic dipole that can hybridize with the electric dipole of a plasmonic structure to produce a very rich response

Si cylinder



Si cylinder + Ag disk

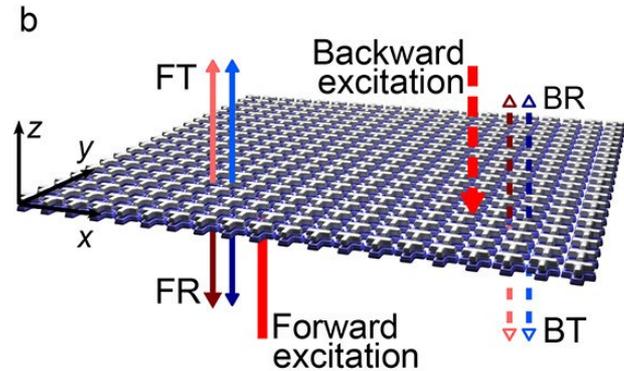
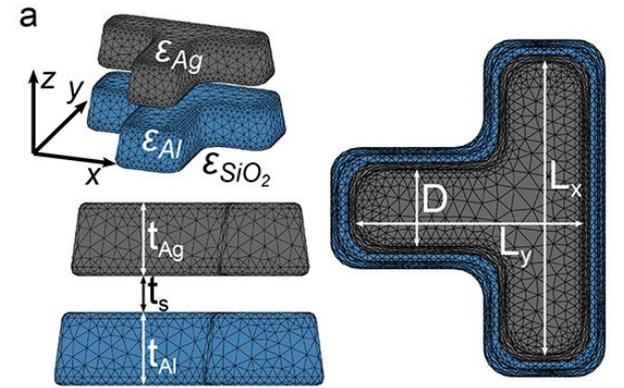
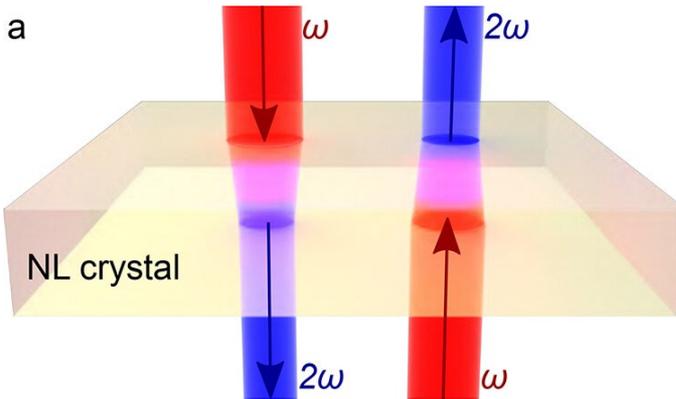
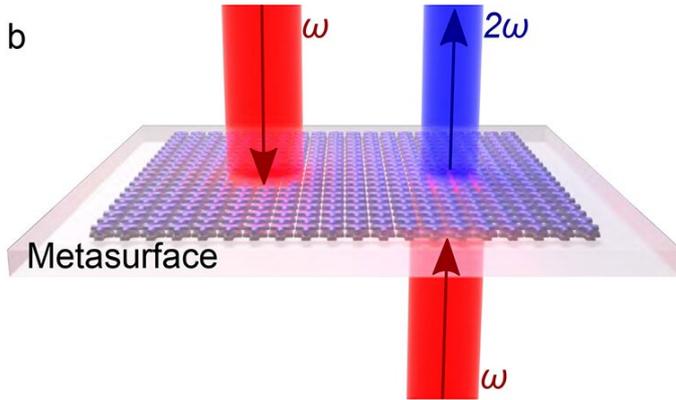


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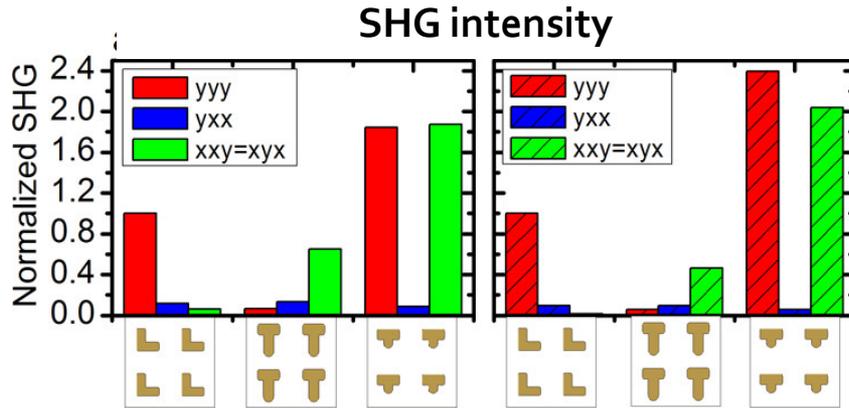
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# Asymmetric nonlinear metasurface – Meta-atom design

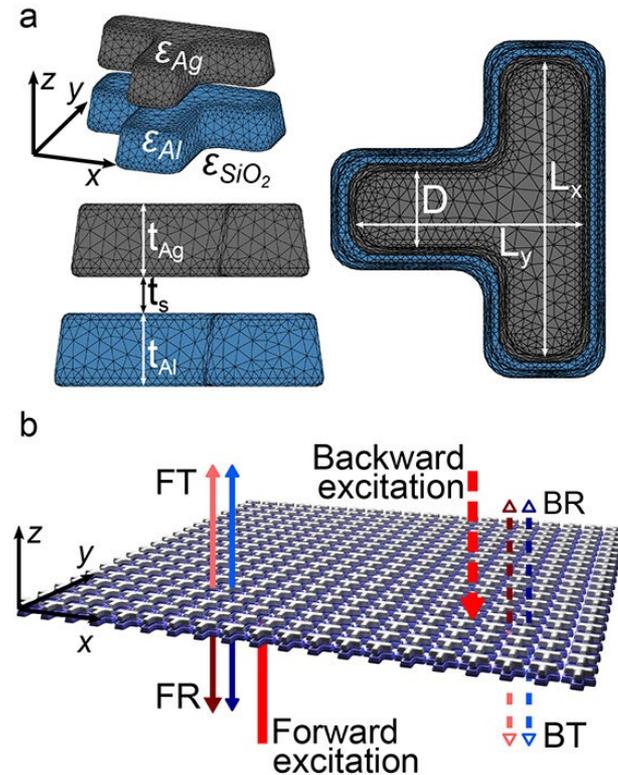


# Asymmetric nonlinear metasurface – Meta-atom design

- T-shape plasmonic nanostructure
- Excitation polarization along the x-direction
- SHG produced along the y-direction

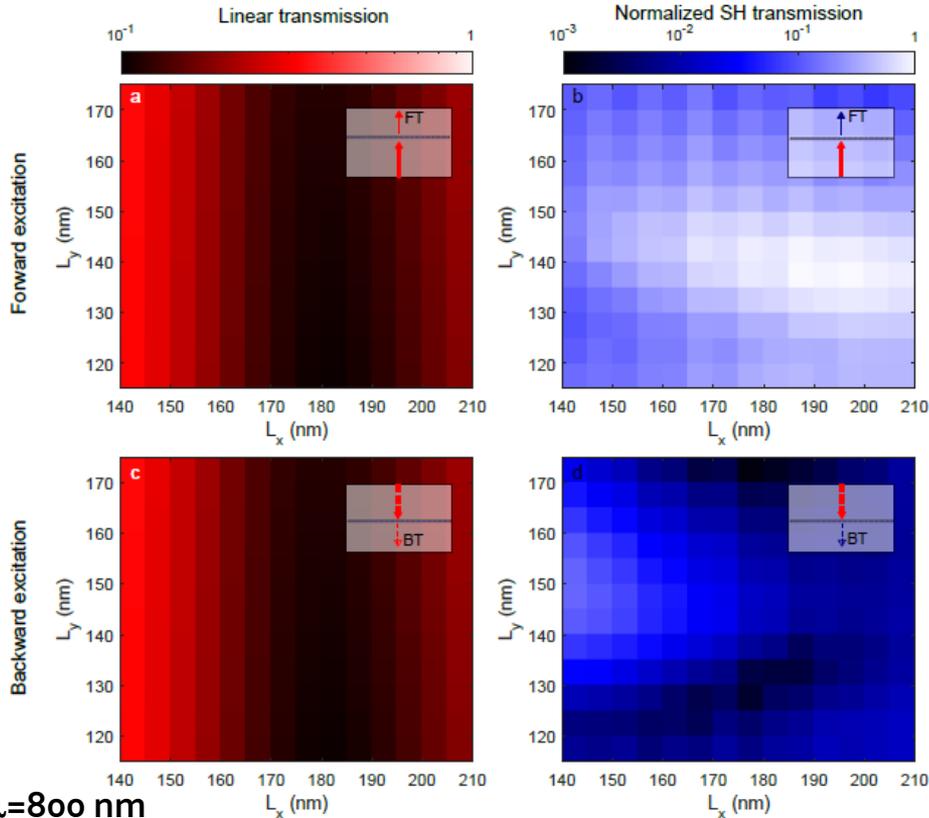


*R. Czaplicki, Nano Letters vol. 15, p. 530 (2015)*



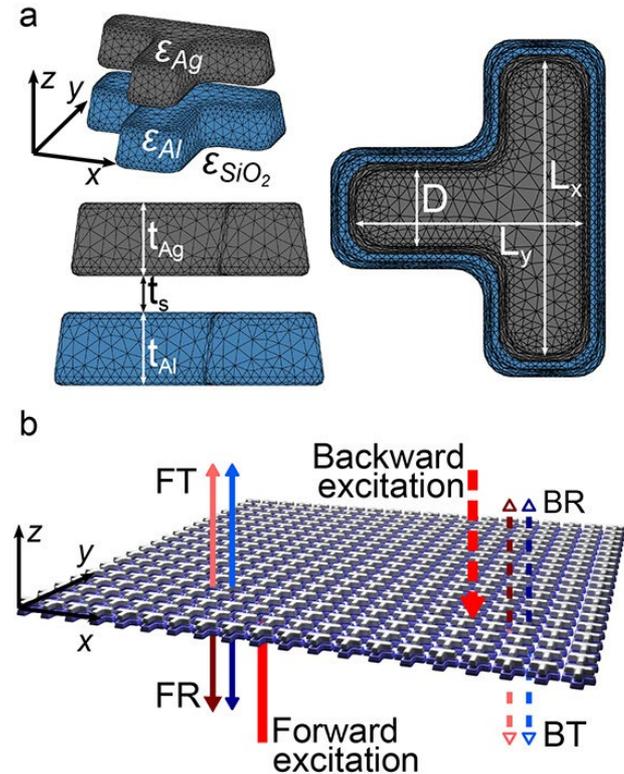
# Asymmetric nonlinear metasurface – Meta-atom design

- A T-shape provides independent control for the resonances at  $\omega$  and  $2\omega$



$\lambda=800$  nm

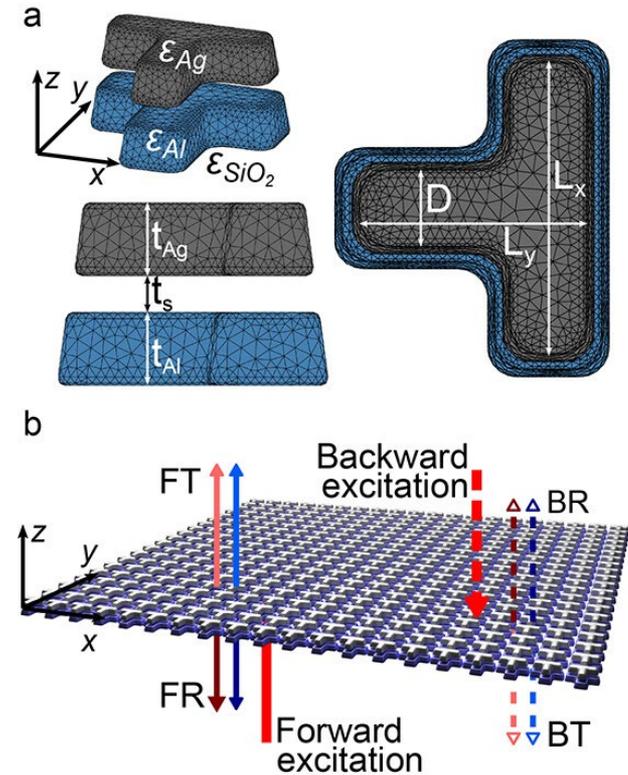
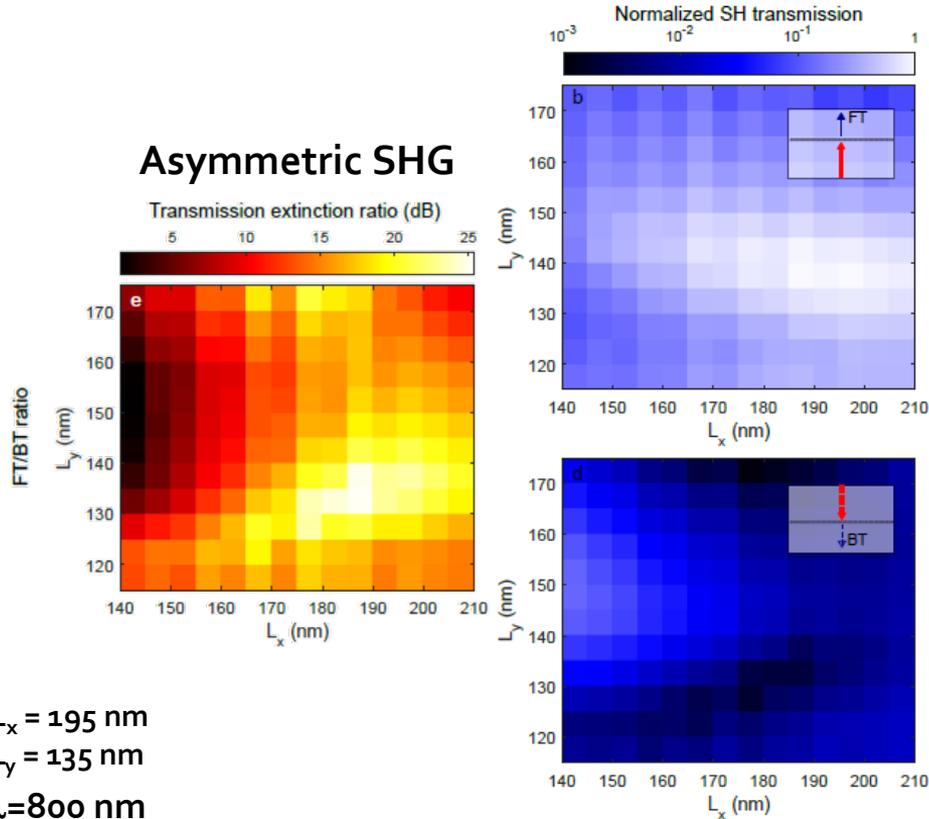
www.nanophotonics.ch



S. Boroviks, *Nano Letters*, vol. 23, p. 3362 (2023)

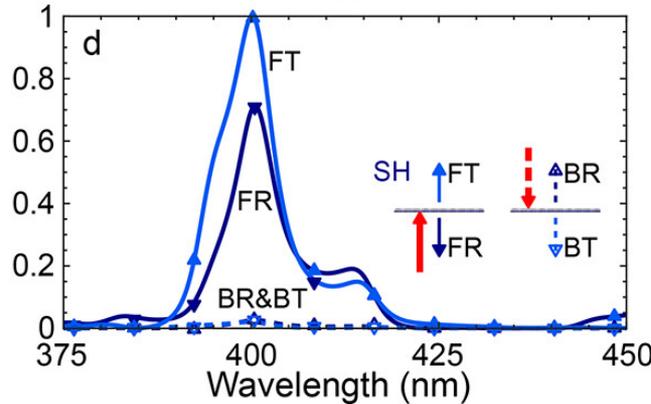
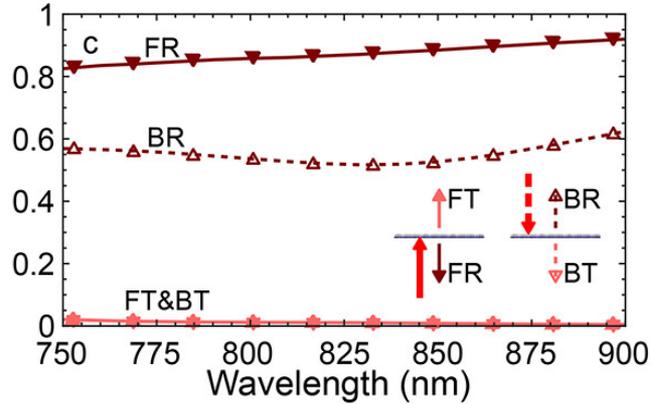
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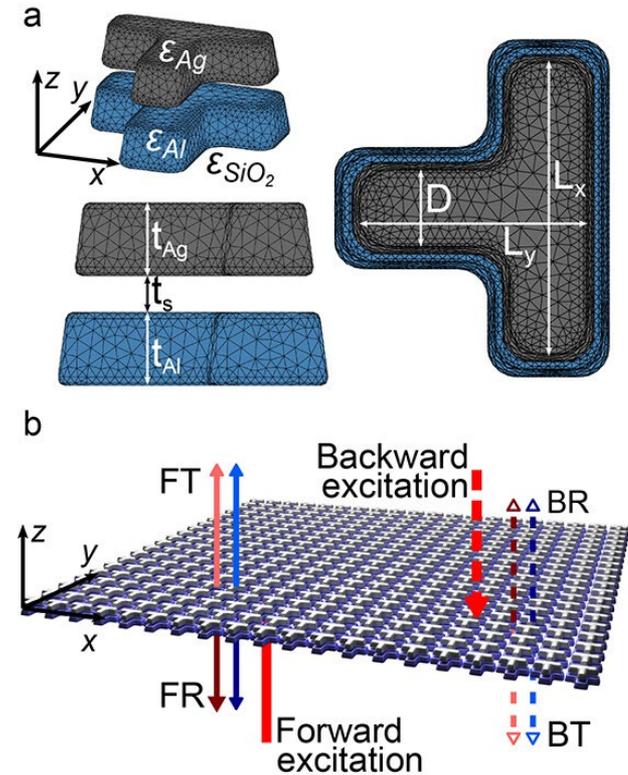


# Asymmetric nonlinear metasurface – Meta-atom design

- Numerical simulations in the linear and nonlinear regimes

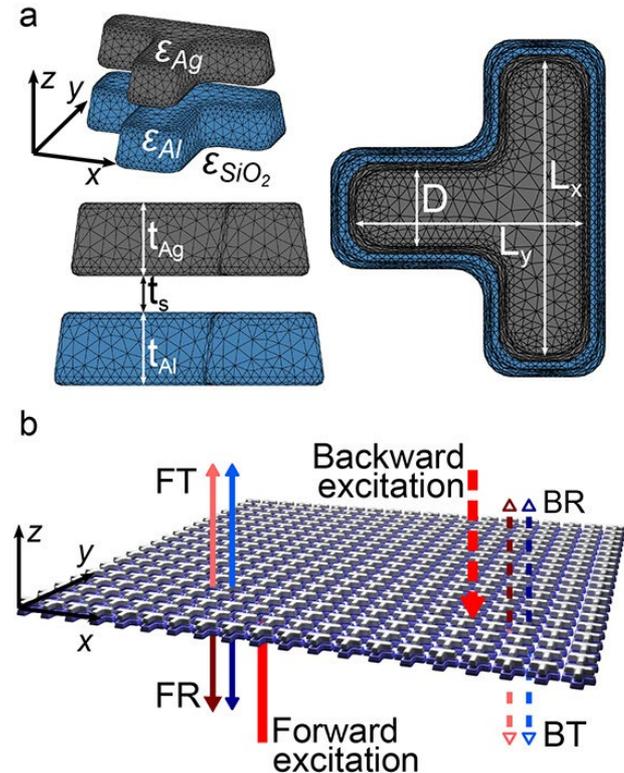


$L_x = 195$  nm  
 $L_y = 135$  nm



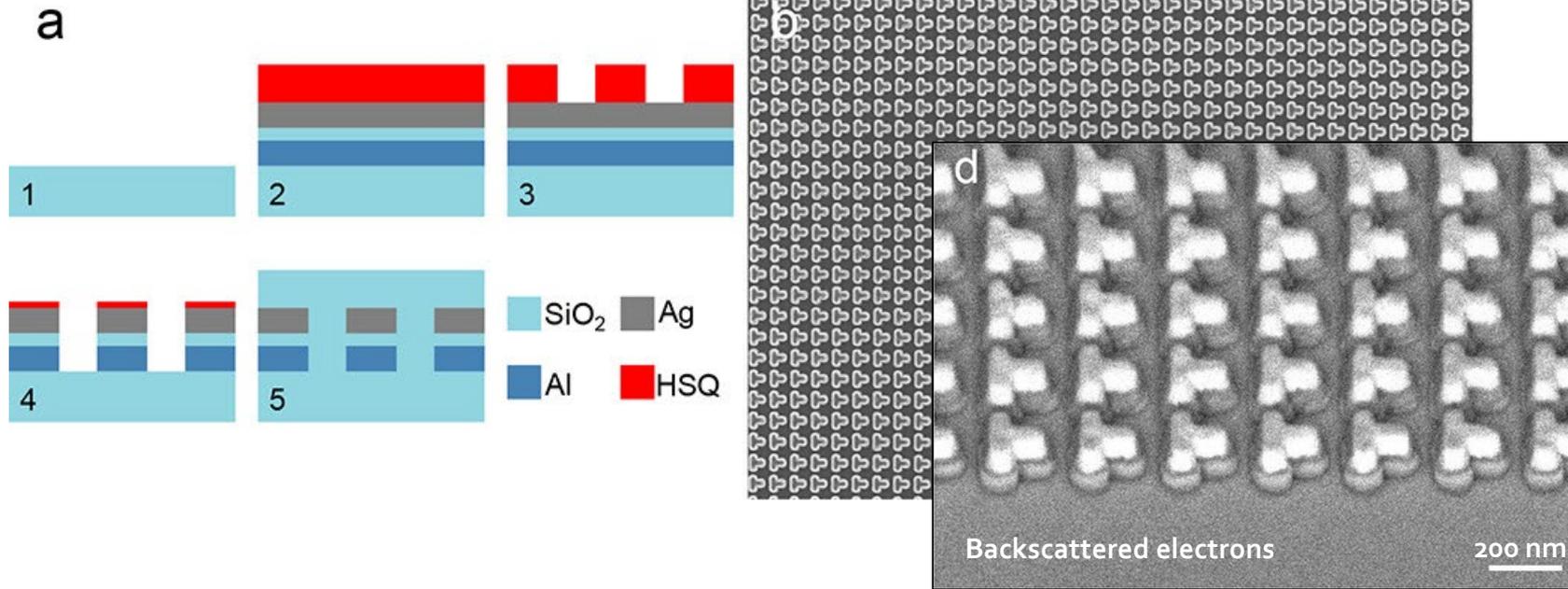
# Nanofabrication

- Array of Al – Ag meta-atoms (each 50 nm thick)
- $L_x = 195$  nm,  $L_y = 135$  nm
- Square lattice with period  $\Lambda = 250$  nm (avoid diffraction orders at  $\omega$  and  $2\omega$ )
- 25 nm  $\text{SiO}_2$  spacer ( $n = 1.49$ )
- Embedded in  $\text{SiO}_2$  (symmetric environment)



# Strongly asymmetric SHG – Nanofabrication using ion etching (Ar)

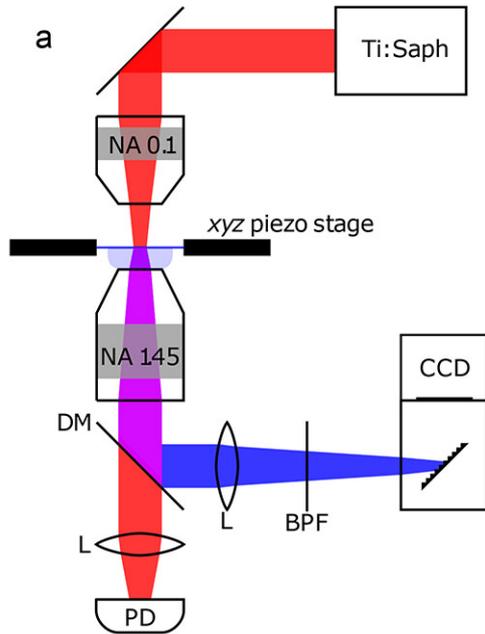
- HSQ mask used for ion etching (Ar) the nanostructures



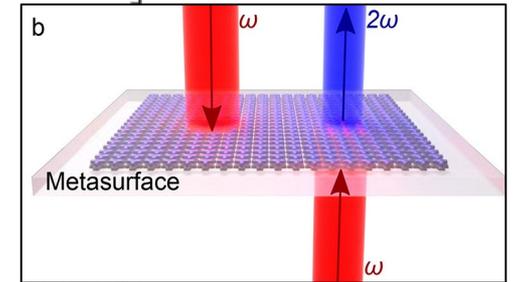
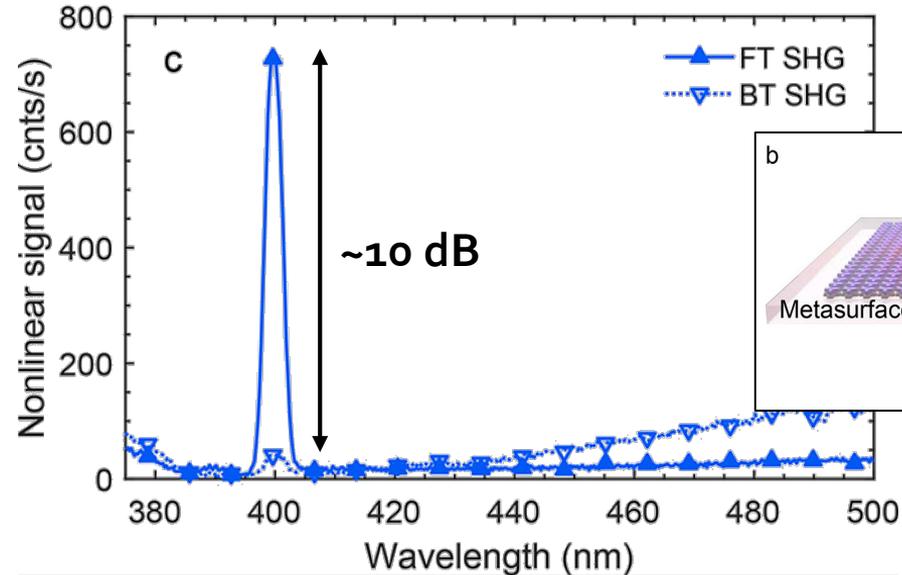
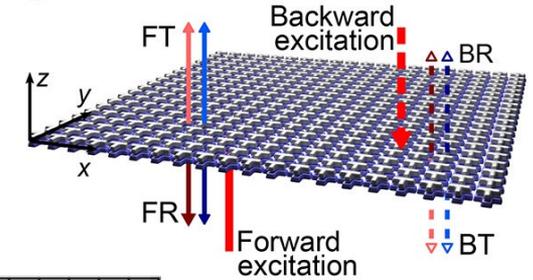
*S. Boroviks, Nano Letters, vol. 23, p. 3362 (2023)*

*B. Abasahl, Nanotechnology vol. 32, p. 475202 (2021)*

# Experimental characterization

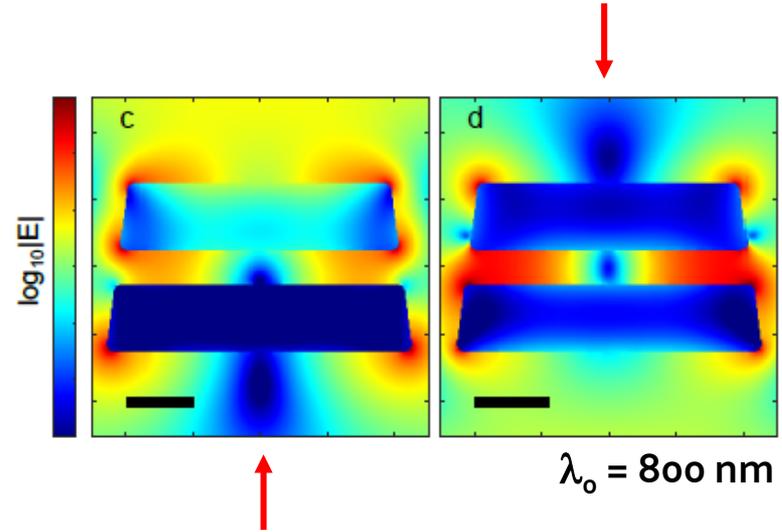
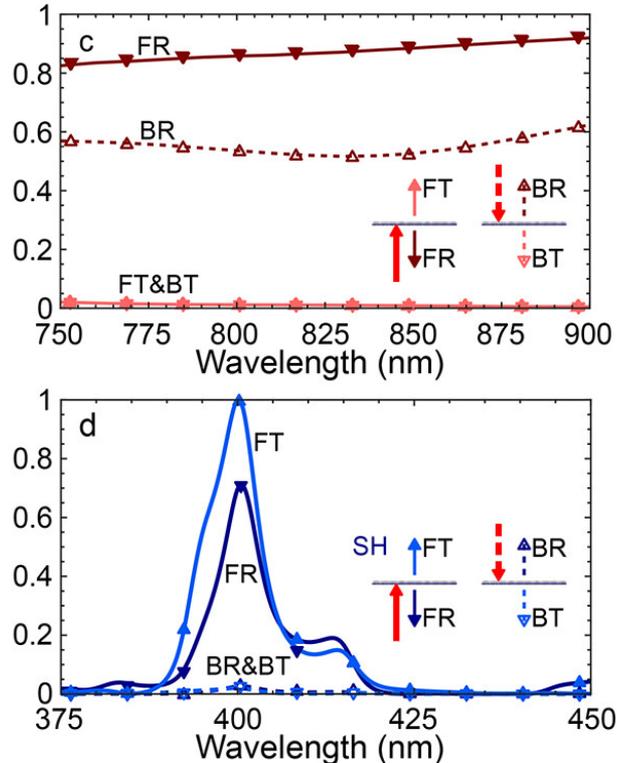


$\lambda_0 = 800 \text{ nm}$   
120 fs pulse duration



# How does it work?

- Different field distributions depending on the illumination direction
- Bianisotropy (magneto-electric coupling), asymmetric absorption



## How does it work?

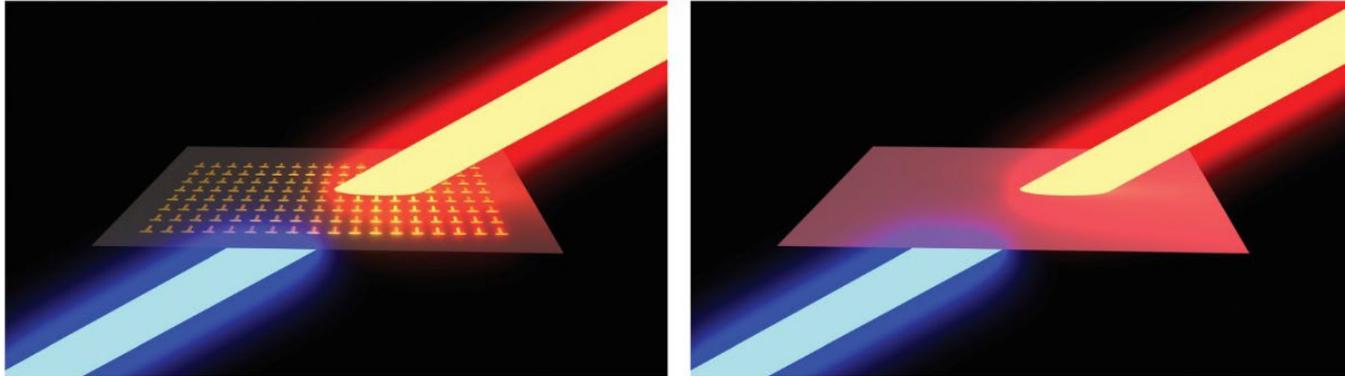
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- Induced linear and nonlinear polarizations

$$\mathbf{P}^{\omega} = \bar{\bar{\chi}}_{ee}^{\omega} \cdot \mathbf{E}^{\omega} + \bar{\bar{\chi}}_{em}^{\omega} \cdot \mathbf{H}^{\omega}$$

$$\mathbf{P}^{2\omega} = \bar{\bar{\chi}}_{ee}^{2\omega} \cdot \mathbf{E}^{2\omega} + \bar{\bar{\chi}}_{em}^{2\omega} \cdot \mathbf{H}^{2\omega} + \bar{\bar{\chi}}_{eee}^{\omega} : \mathbf{E}^{\omega} \mathbf{E}^{\omega} + \bar{\bar{\chi}}_{eem}^{\omega} : \mathbf{E}^{\omega} \mathbf{H}^{\omega} + \bar{\bar{\chi}}_{emm}^{\omega} : \mathbf{H}^{\omega} \mathbf{H}^{\omega}$$

- Retrieved numerically – Homogenization procedure based on the generalized sheet transition conditions (GSTCs)



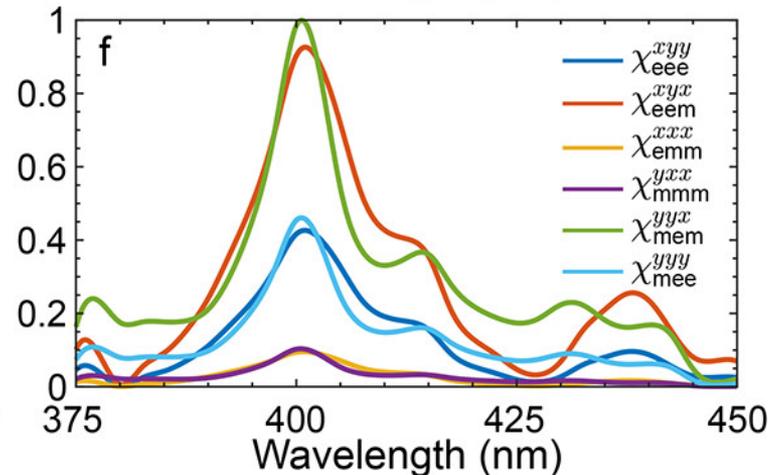
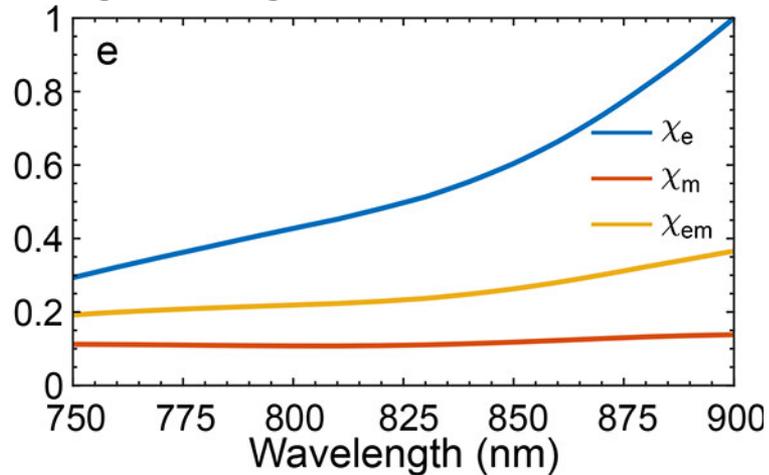
# How does it work?

- Induced linear and nonlinear polarizations

$$\mathbf{P}^{\omega} = \bar{\chi}_{ee}^{\omega} \cdot \mathbf{E}^{\omega} + \bar{\chi}_{em}^{\omega} \cdot \mathbf{H}^{\omega}$$

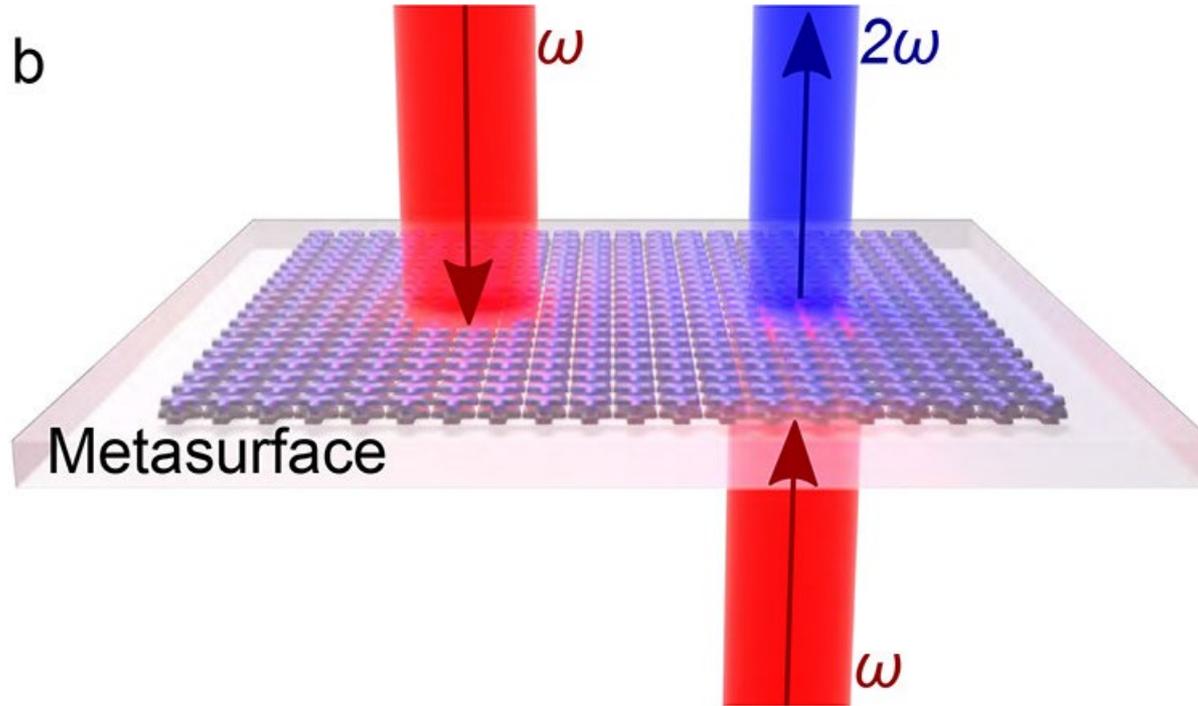
$$\mathbf{P}^{2\omega} = \bar{\chi}_{ee}^{2\omega} \cdot \mathbf{E}^{2\omega} + \bar{\chi}_{em}^{2\omega} \cdot \mathbf{H}^{2\omega} + \bar{\chi}_{eee}^{\omega} : \mathbf{E}^{\omega} \mathbf{E}^{\omega} + \bar{\chi}_{eem}^{\omega} : \mathbf{E}^{\omega} \mathbf{H}^{\omega} + \bar{\chi}_{emm}^{\omega} : \mathbf{H}^{\omega} \mathbf{H}^{\omega}$$

- Linear regime: non negligible magneto-electric coupling term  $\chi_{em}$
- Nonlinear susceptibilities dominated by magnetic/electric excitations along orthogonal directions  $\chi_{eem}^{xyx}$ ,  $\chi_{mem}^{yyx}$



# Is it nonreciprocal?

---



## Electromagnetic Nonreciprocity

Christophe Caloz,<sup>1,\*</sup> Andrea Alù,<sup>2</sup> Sergei Tretyakov,<sup>3</sup> Dimitrios Sounas,<sup>4</sup> Karim Achouri,<sup>5</sup> and Zoé-Lise Deck-Léger<sup>1</sup>

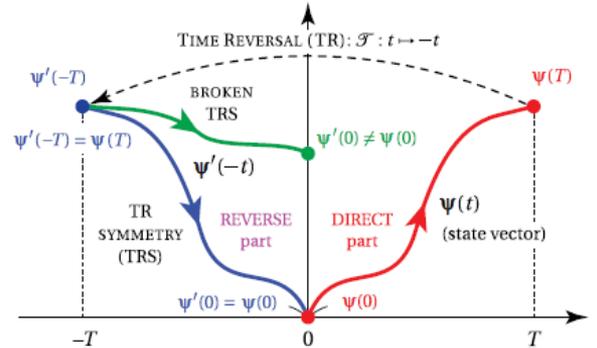
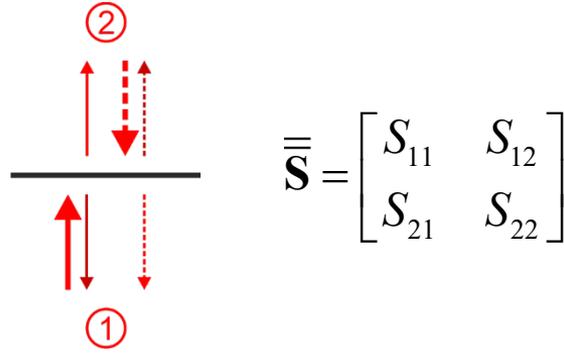


FIG. 1. Time-reversal symmetry (TRS) (red and blue curves) and broken time-reversal symmetry (red and green curves), or time-reversal asymmetry, as a general thought experiment and mathematical criterion for nonreciprocity.

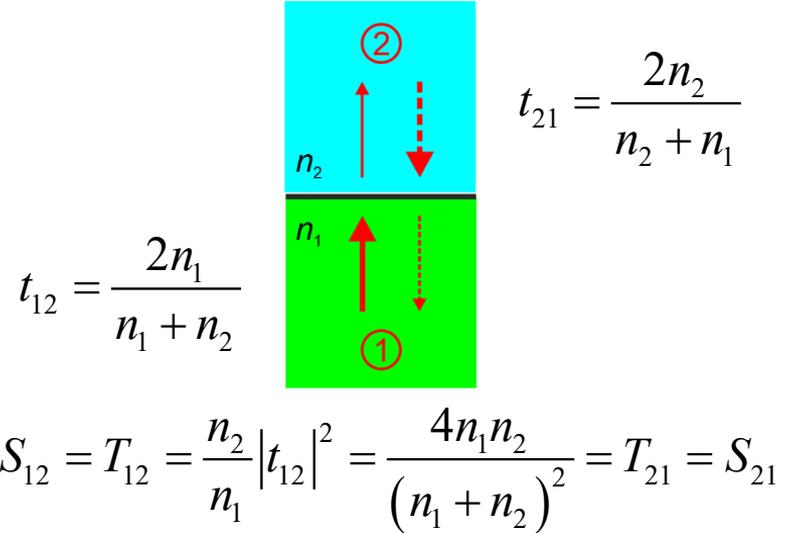
# Is it nonreciprocal?

- Linear regime: 2-port system



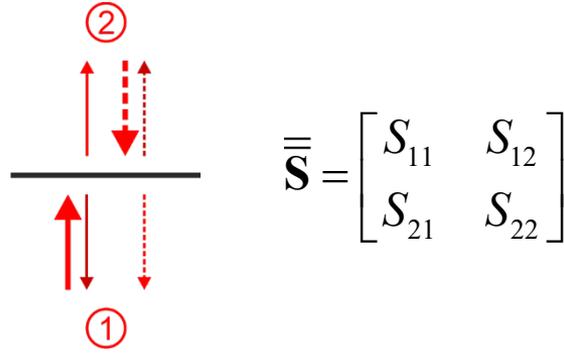
- Reciprocity requires  $\bar{\mathbf{S}} = \bar{\mathbf{S}}^T$
- Equal transmission coefficients  $S_{12} = S_{21}$
- No constraints on the reflection coefficients  $S_{11}, S_{22}$

- Fresnel coefficients

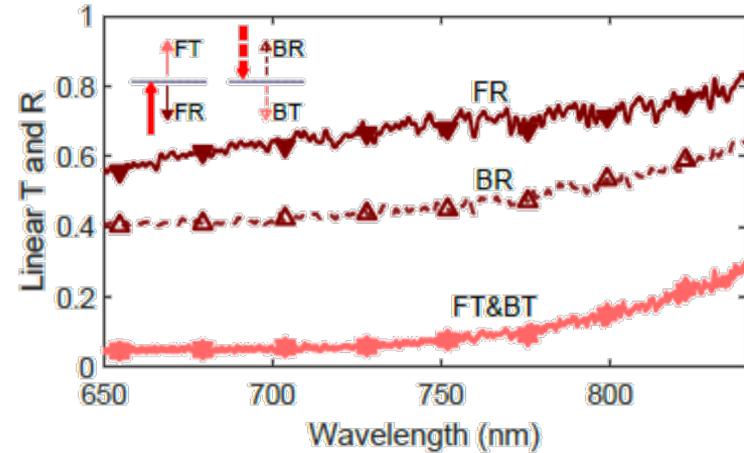


# Is it nonreciprocal?

- Linear regime: 2-port system

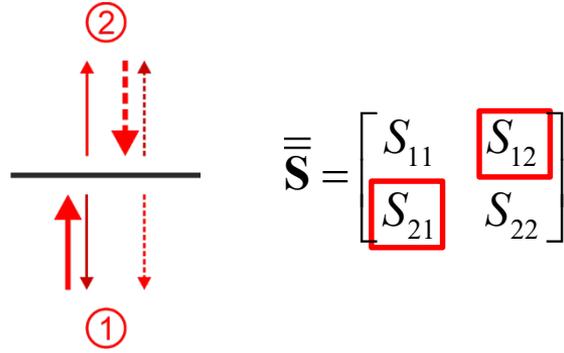


- Reciprocity requires  $\bar{\mathbf{S}} = \bar{\mathbf{S}}^T$
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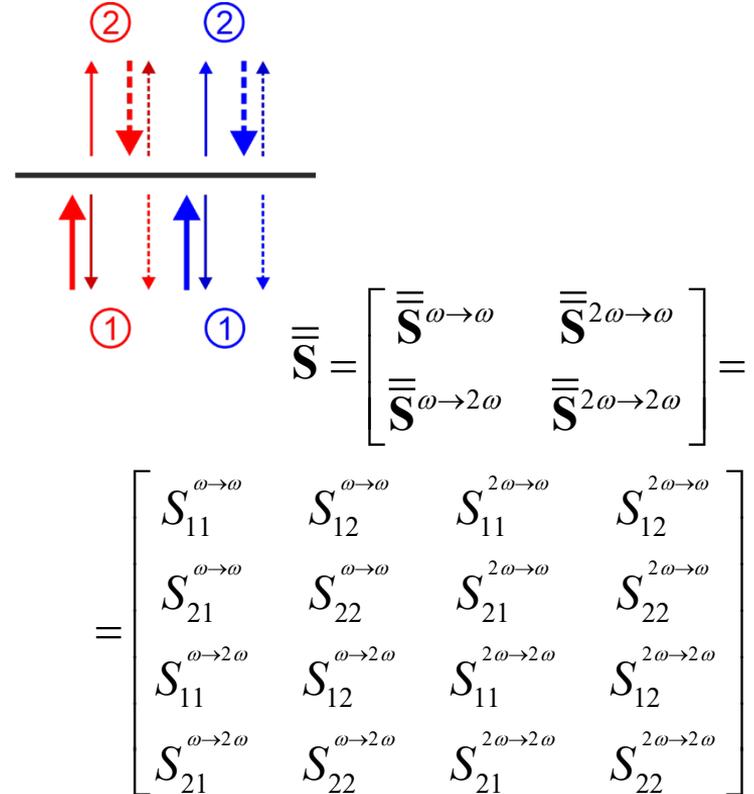
# Is it nonreciprocal?

- Linear regime: 2-port system



- Reciprocity requires  $\bar{\mathbf{S}} = \bar{\mathbf{S}}^T$
- Equal transmission coefficients  $S_{12} = S_{21}$
- No constraints on the reflection coefficients  $S_{11}, S_{22}$

- Nonlinear regime: 4-port system



# Is it nonreciprocal?

- Probing (non)reciprocity would require probing six (in)equalities:

$$S_{21}^{\omega \rightarrow \omega} \stackrel{?}{=} S_{12}^{\omega \rightarrow \omega} \quad S_{12}^{\omega \rightarrow 2\omega} \stackrel{?}{=} S_{21}^{2\omega \rightarrow \omega}$$

$$S_{11}^{\omega \rightarrow 2\omega} \stackrel{?}{=} S_{11}^{2\omega \rightarrow \omega} \quad S_{22}^{\omega \rightarrow 2\omega} \stackrel{?}{=} S_{22}^{2\omega \rightarrow \omega}$$

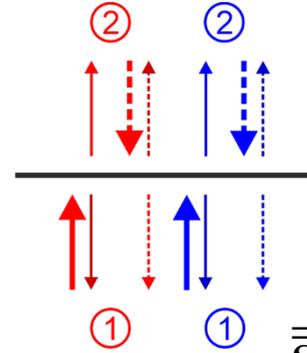
$$S_{21}^{\omega \rightarrow 2\omega} \stackrel{?}{=} S_{12}^{2\omega \rightarrow \omega} \quad S_{21}^{2\omega \rightarrow 2\omega} \stackrel{?}{=} S_{12}^{2\omega \rightarrow 2\omega}$$

- So far, we have only shown that

$$S_{21}^{\omega \rightarrow 2\omega} \neq S_{12}^{\omega \rightarrow 2\omega}$$

(asymmetric nonlinear process)

- Nonlinear regime: 4-port system

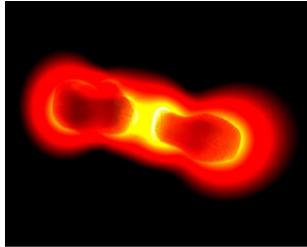


$$\bar{S} \equiv \begin{bmatrix} \bar{S}^{\omega \rightarrow \omega} & \bar{S}^{2\omega \rightarrow \omega} \\ \bar{S}^{\omega \rightarrow 2\omega} & \bar{S}^{2\omega \rightarrow 2\omega} \end{bmatrix} =$$

$$= \begin{bmatrix} S_{11}^{\omega \rightarrow \omega} & S_{12}^{\omega \rightarrow \omega} & S_{11}^{2\omega \rightarrow \omega} & S_{12}^{2\omega \rightarrow \omega} \\ S_{21}^{\omega \rightarrow \omega} & S_{22}^{\omega \rightarrow \omega} & S_{21}^{2\omega \rightarrow \omega} & S_{22}^{2\omega \rightarrow \omega} \\ S_{11}^{\omega \rightarrow 2\omega} & S_{12}^{\omega \rightarrow 2\omega} & S_{11}^{2\omega \rightarrow 2\omega} & S_{12}^{2\omega \rightarrow 2\omega} \\ S_{21}^{\omega \rightarrow 2\omega} & S_{22}^{\omega \rightarrow 2\omega} & S_{21}^{2\omega \rightarrow 2\omega} & S_{22}^{2\omega \rightarrow 2\omega} \end{bmatrix}$$

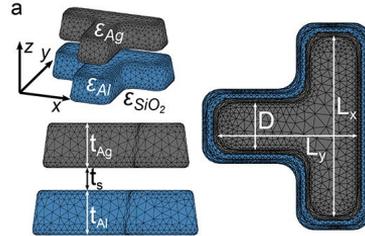
# Summary

Use numerical techniques to their full extent



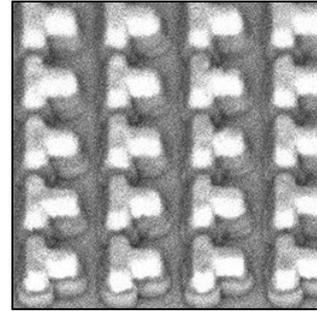
- Model realistic systems
- Perform some numerical experiments that are not feasible in practice

Simple design with strong bianisotropy



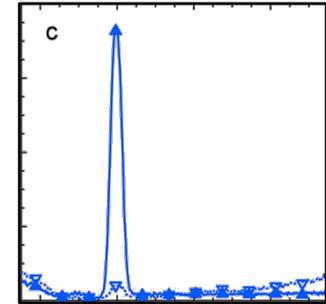
- Easily tunable
- Al and Ag give strong SHG
- Their out-of-plane combination leads to a robust bianisotropy

Simple, versatile nanotechnology



- Dry etching provides very well-defined nanostructures
- It can be used with a diversity of materials

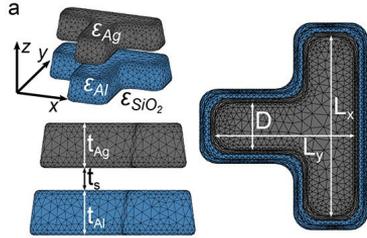
Strong, asymmetric nonlinear response



- 16 dB difference in theory, 10 dB experimentally between forward and backward SHG

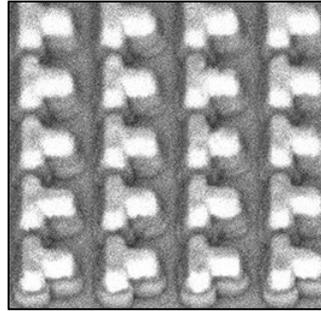
# Summary

Simple design with strong bianisotropy



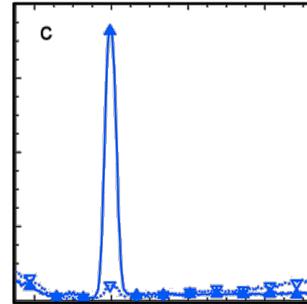
- Easily tunable
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Simple, versatile nanotechnology



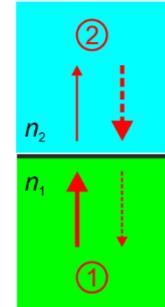
- Dry etching provides very well-defined nanostructures
- It can be used with a diversity of materials

Strong, asymmetric nonlinear response



- 16 dB difference in theory, 10 dB experimentally between forward and backward SHG

No, this is not nonreciprocal!



- The device is time-reversal asymmetric
- Sometimes mistaken with nonreciprocal...

# Acknowledgements

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Sergejs Boroviks



Karim Achouri



Andrei Kiselev



Christian Santschi



**Several post-doc  
positions**