

AI & Law models of case-based reasoning and their applications

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IC3K'25, Marbella
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Information &
Computing
Sciences



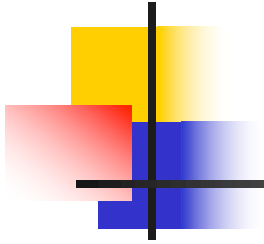
Marek Sergot

Institutional history



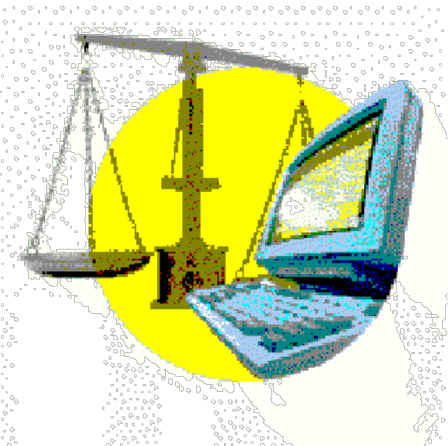
Thorne McCarty

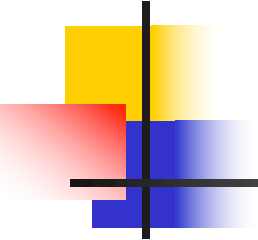
- Florence conferences 1982,1985,1989
- ICAIL conferences since 1987
- JURIX conferences since 1988
- AI & Law journal since 1992
- ...
- Two landmark papers:
 - Taxman (Thorne McCarty, 1977): precedents
 - British Nationality Act (Marek Sergot et al., 1985): legislation



Factor-based reasoning

- In legal classification and interpretation there are often **no clear rules**
- Often there only are factors: **tentative** reasons **pro** or **con** a conclusion
 - Often to different **degrees**
- Factors are weighed in **cases**, which become **precedents**
 - How do judges, solicitors ... then **argue**?
 - And how do precedents **constrain** new decisions?





Example from US law: misuse of trade secrets

- *Some factors pro misuse of trade secrets:*

- F4 Agreed-Not-To-Disclose
- F6 Security-Measures
- F18 Identical-Products
- F21 Knew-Info-Confidential
- ...

- *Some factors con misuse of trade secrets:*

- F1 Disclosure-In-Negotiations
- F16 Info-Reverse-Engineerable
- ...

HYPO

Ashley & Rissland
1985-1990

CATO

Aleven & Ashley
1991-1997

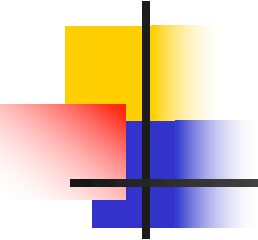
HYPO

Ashley & Rissland 1987-1990



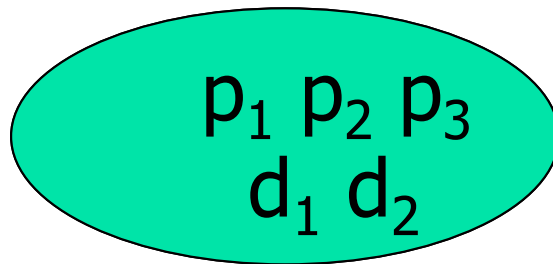
Kevin Ashley &
Edwina Rissland

- Representation language:
 - Cases: π -factors and δ -factors + decision (π or δ)
 - Current Fact Situation: π -factors and δ -factors
- Arguments:
 - Citing (for its decision) a case on its similarities with CFS
 - Distinguishing a case on its differences with CFS
 - Taking into account which side is favoured by a factor

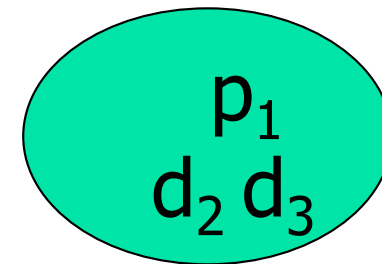


Example with factors

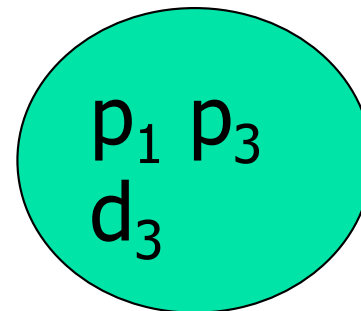
$C_1 (\pi)$

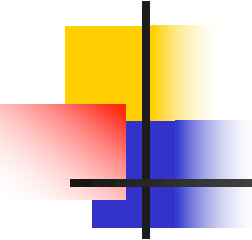


$C_2 (\delta)$



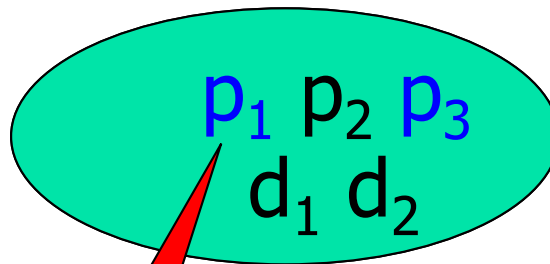
CFS





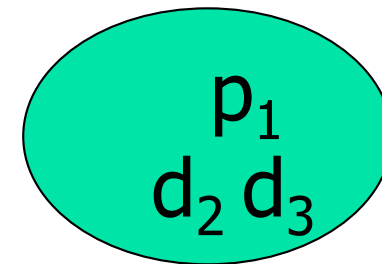
Example with factors

$C_1 (\pi)$

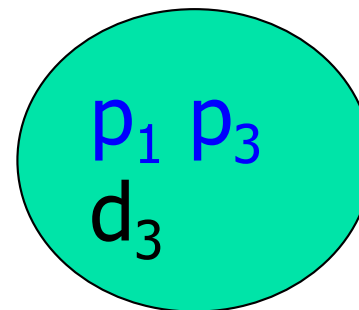


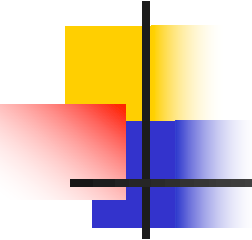
Cite for π

$C_2 (\delta)$



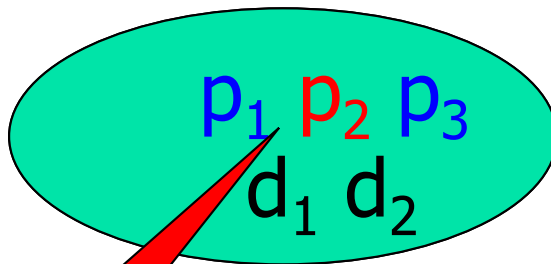
CFS





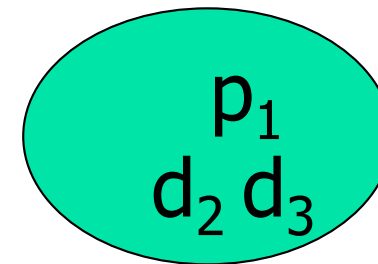
Example with factors

$C_1 (\pi)$

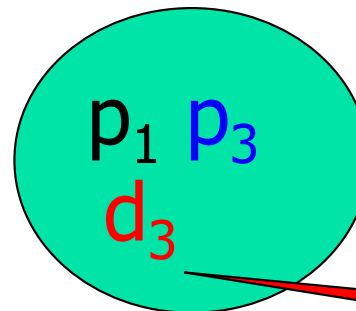


Distinguish!

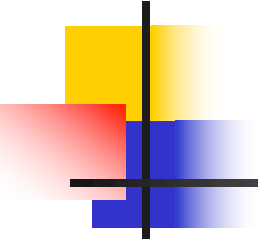
$C_2 (\delta)$



CFS

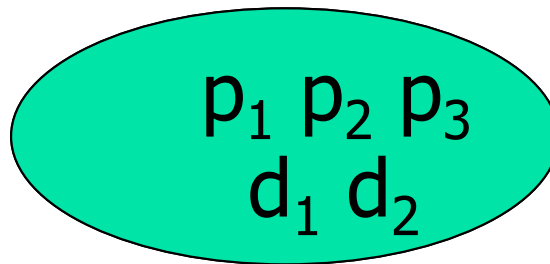


Distinguish!

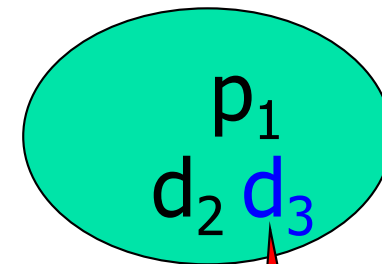


Example with factors

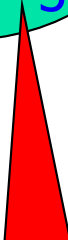
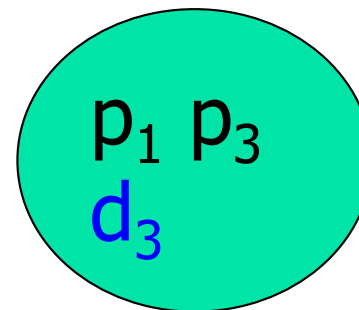
$C_1 (\pi)$



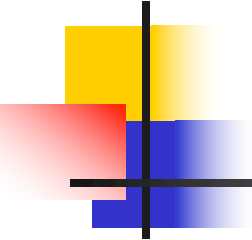
$C_2 (\delta)$



CFS

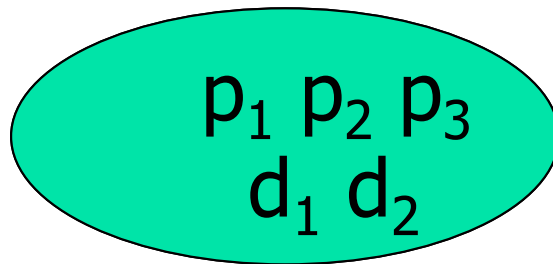


Cite for δ

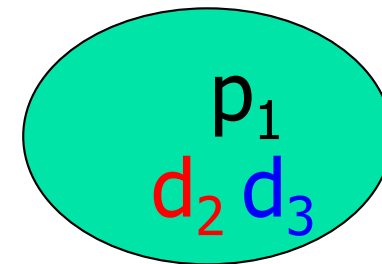


Example with factors

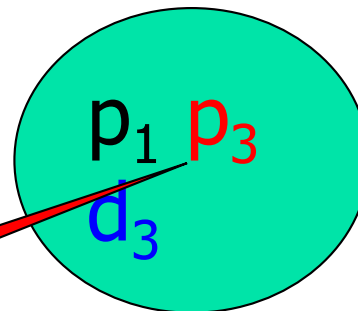
$C_1 (\pi)$



$C_2 (\delta)$

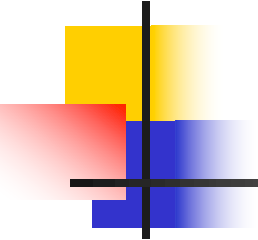


CFS



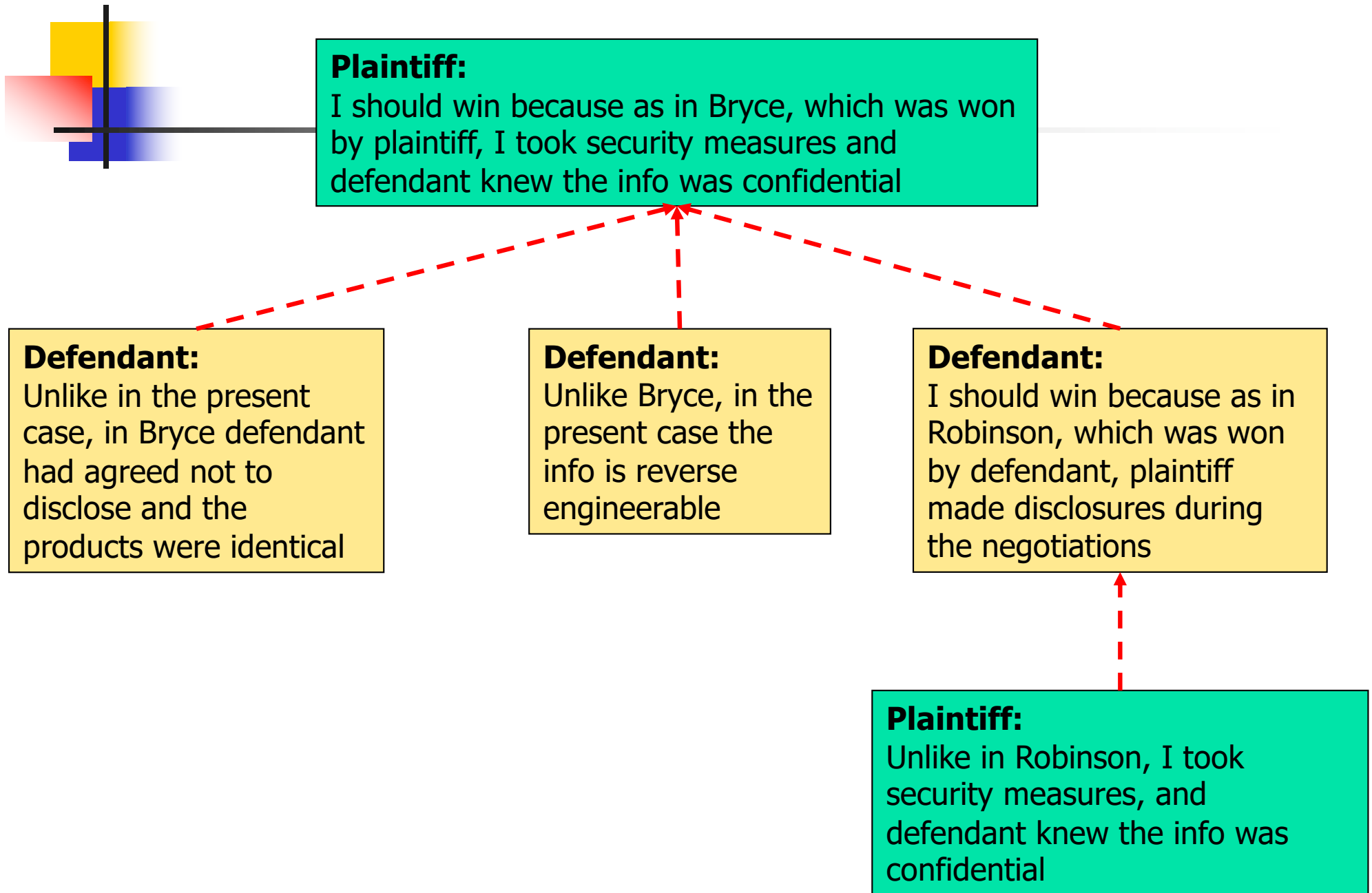
Distinguish!

Distinguish!



HYPO's argument game

- **Given:** a case base and a current fact situation
- Plaintiff starts with a **citable case**
 - A case decided for plaintiff and sharing pro-plaintiff factors with the CFS
- Defendant:
 - cites all **counterexamples** (cases citable for defendant)
 - **distinguishes** citation in all possible ways
 - On pro-plaintiff factors of precedent lacking in CFS
 - On new pro-defendant factors in the CFS
- Plaintiff distinguishes defendant's counterexamples in all possible ways





Vincent Aleven 1991-1997

(snapshot of)
CATO Factor
Hierarchy

Misuse of Trade
Secret (p)

F120: Info legitimately
obtained elsewhere (d)

F101: Info Trade Secret (p)

F102: Efforts to maintain
secrecy (p)

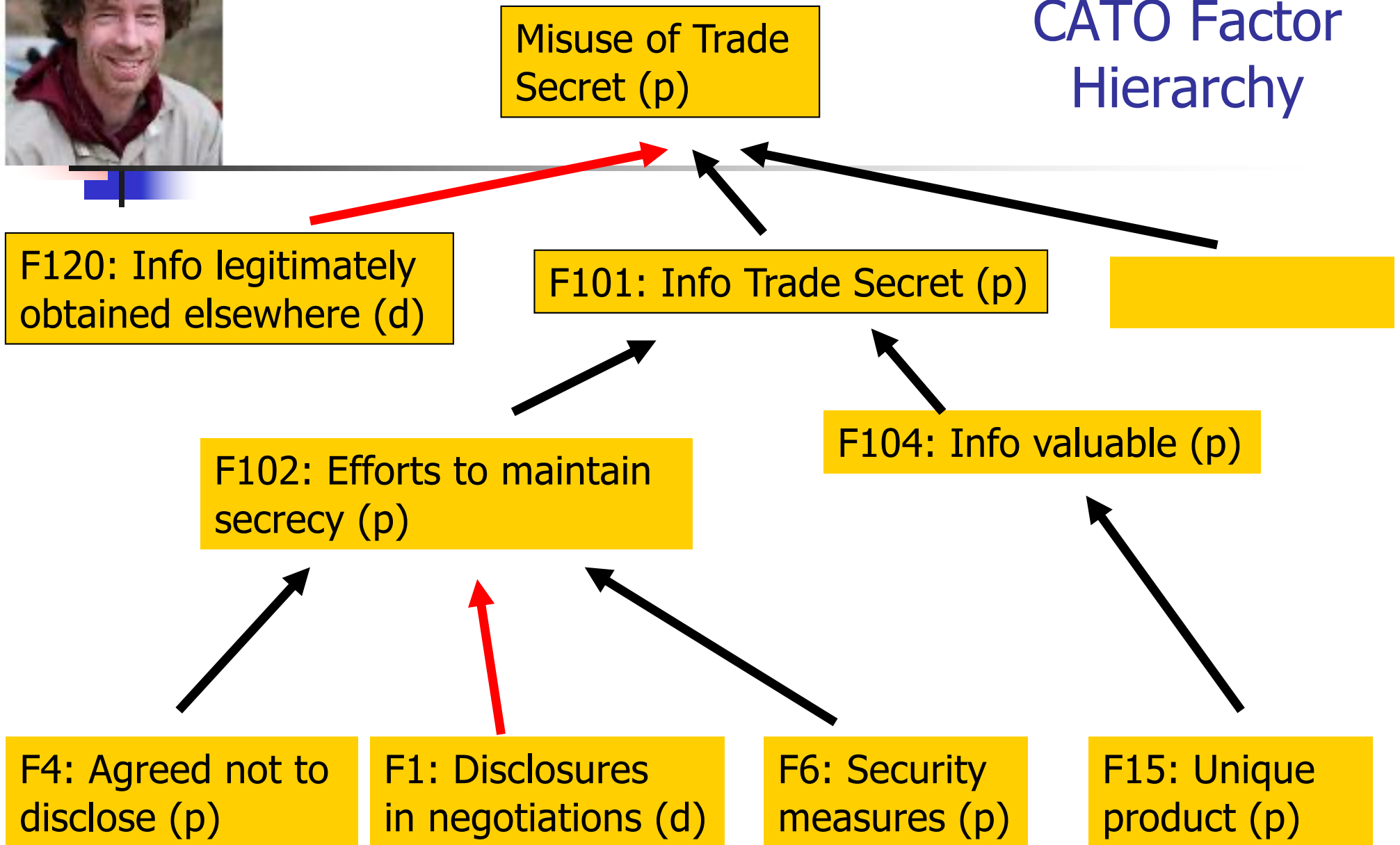
F104: Info valuable (p)

F4: Agreed not to
disclose (p)

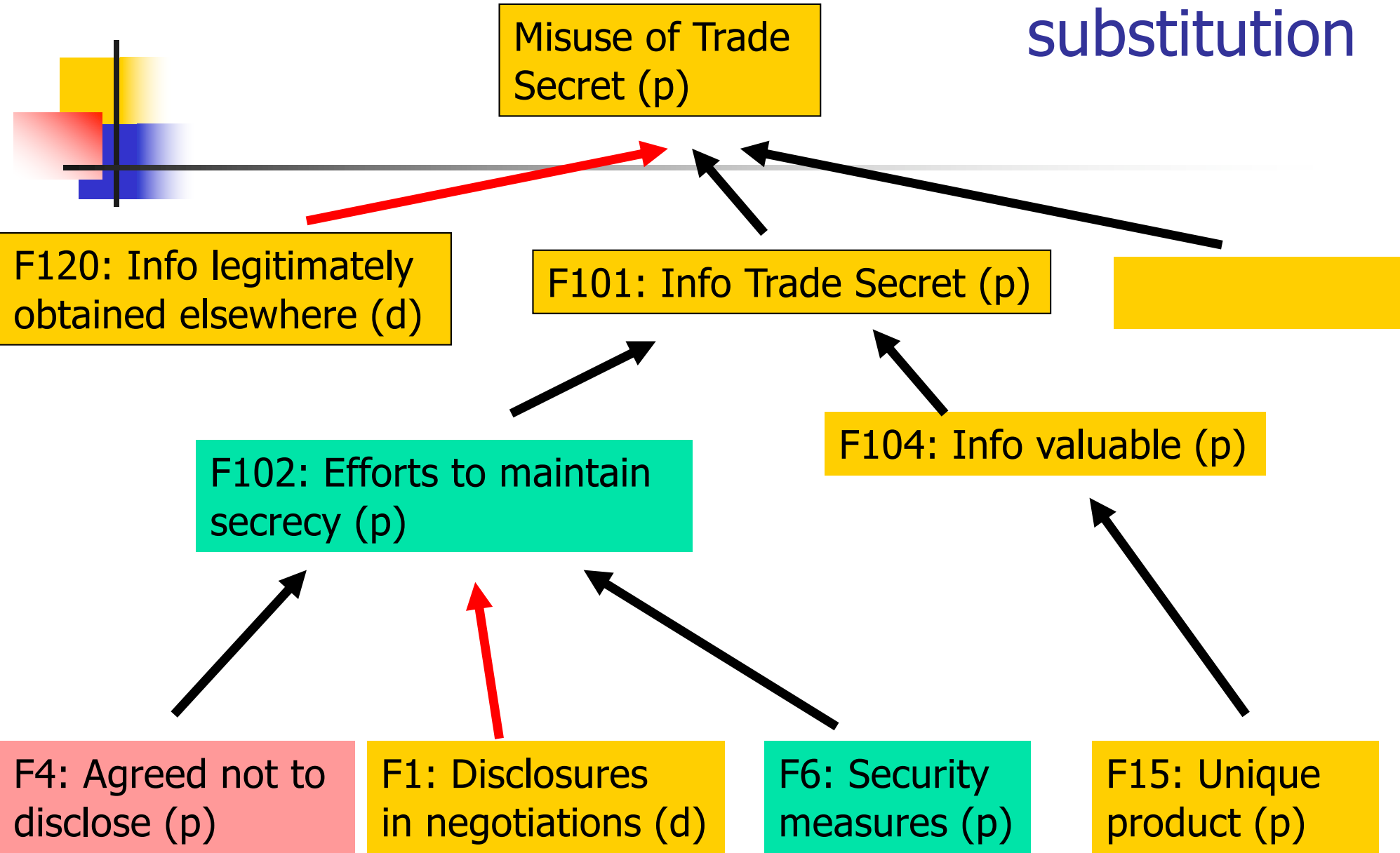
F1: Disclosures
in negotiations (d)

F6: Security
measures (p)

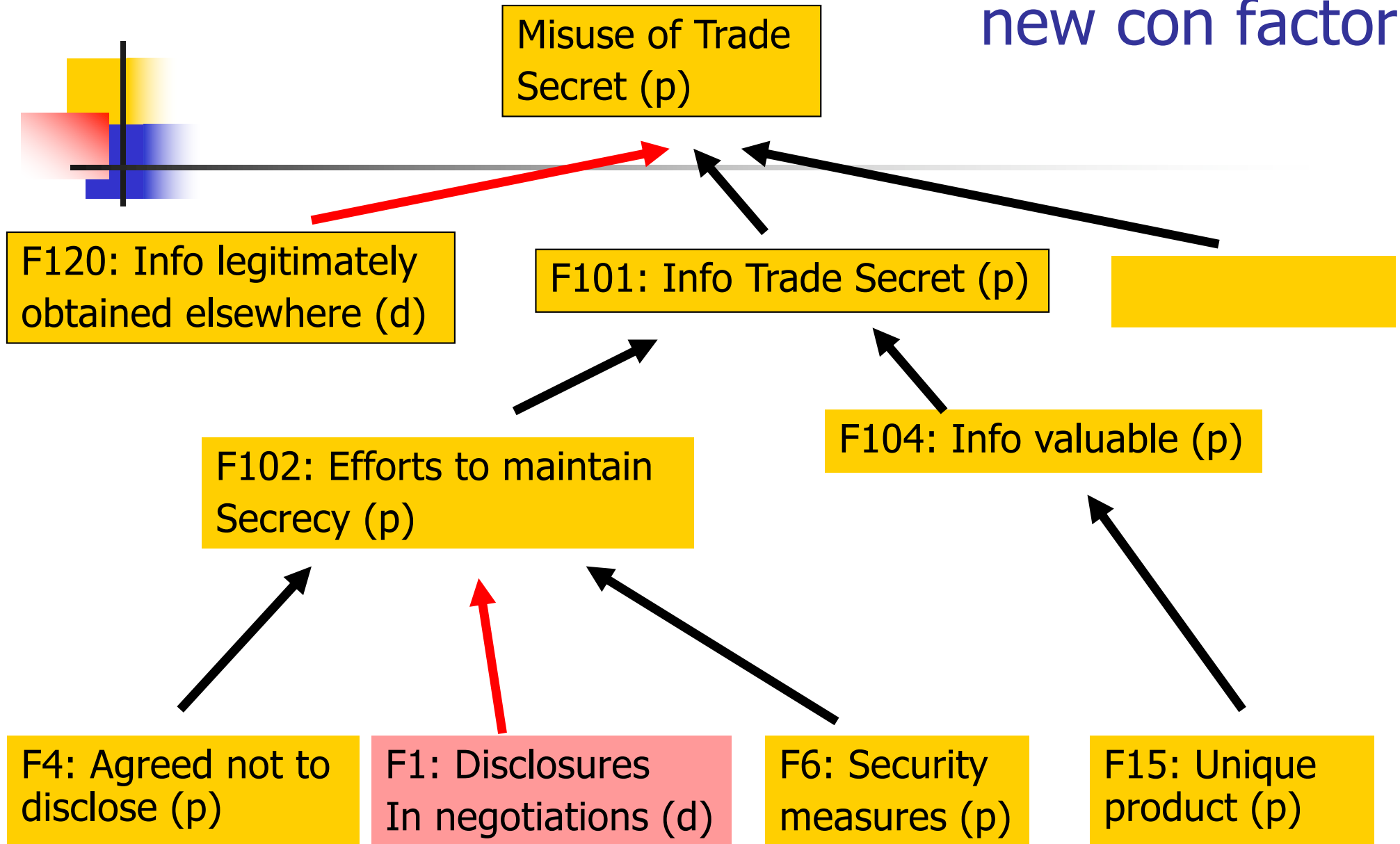
F15: Unique
product (p)



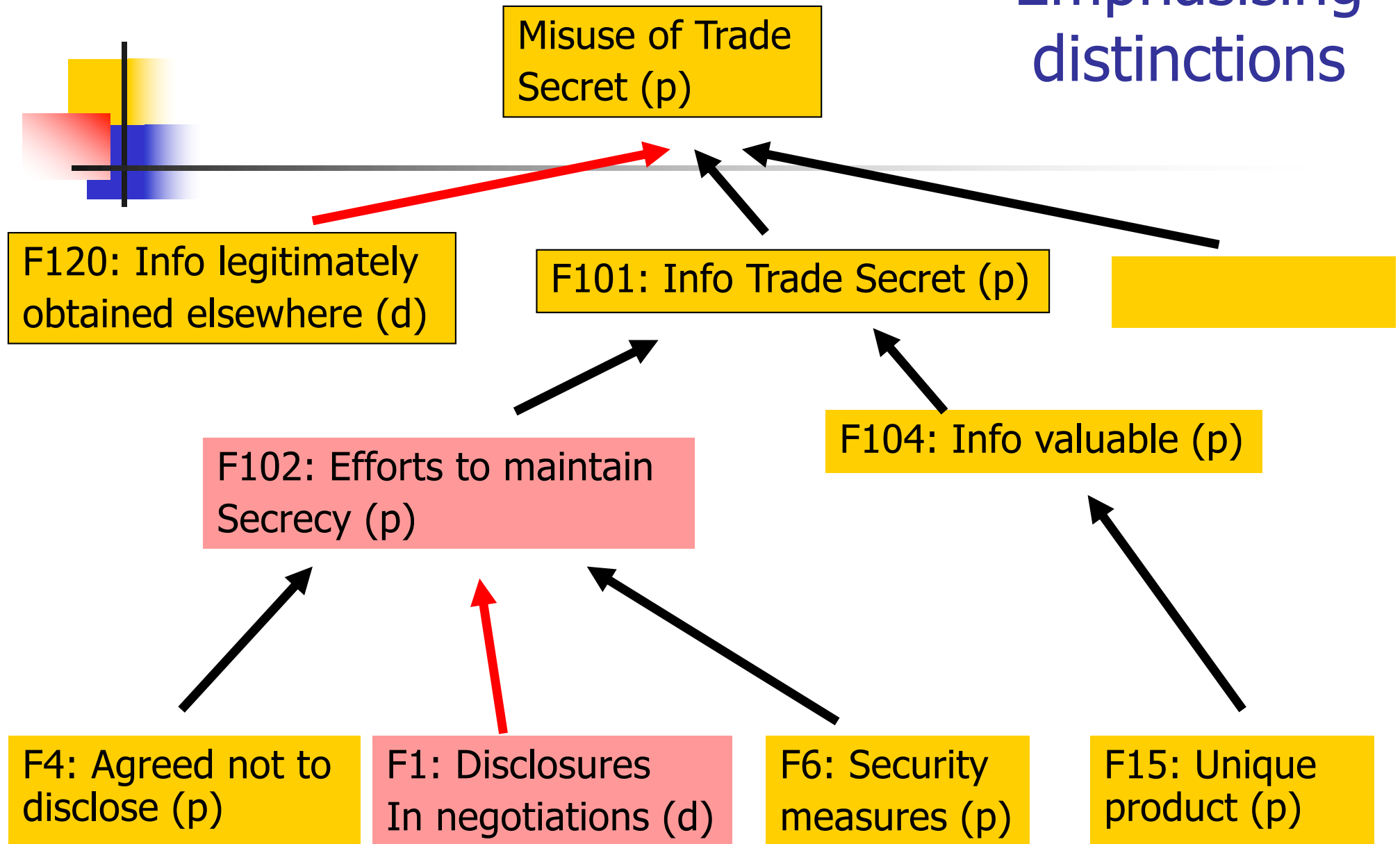
Downplaying by substitution



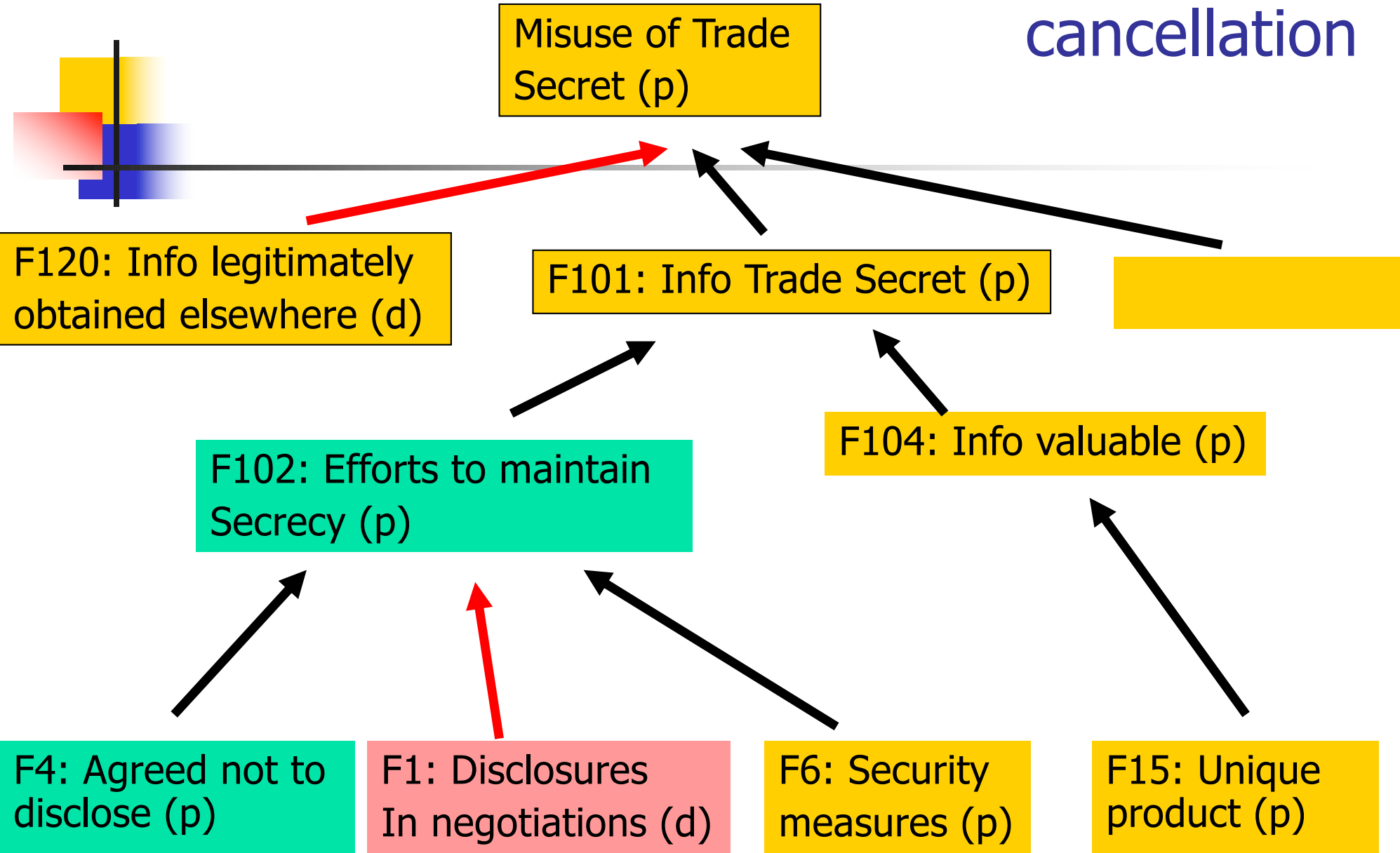
Distinguishing on new con factor

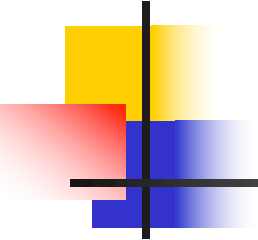


Emphasising distinctions



Downplaying by cancellation





Later developments

- Combining **rules** and **cases**
 - Cabaret (Rissland & Skalak 1989-1991)
 - IBP (Ashley & Brüninghaus 2003-2009)
- Underlying **values**
 - many since Berman & Hafner 1993, Bench-Capon 2000
- **Theory construction**
 - Bench-Capon & Sartor 2001, Bench-Capon & Chorley 2003-2006
- Precedential **constraint**
 - Horty 2011-, ...

Trevor Bench-Capon





Precedential constraint

- When is a decision in a new case 'forced' by a case base?
 - If the case base contains a precedent for that decision that **cannot be distinguished**:
 - All differences make the new case even stronger for the new decision

J. Horty, Rules and reasons in the theory of precedent. *Legal Theory* 17 (2011): 1-33.

...

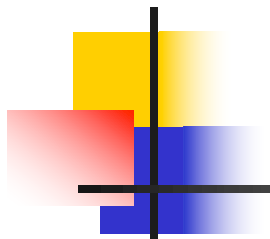
H. Prakken, A formal analysis of some factor- and dimension-based accounts of precedential constraint. *Artificial Intelligence and Law* 29 (2021): 559-585.

...

the factors in G
favouring s
(the pro s factors)

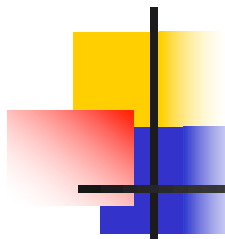
Result model with factors

- For two **fact situations** F and G and **sides** s, -s:
- $G \leq_s F$ iff $G^s \subseteq F^s$ and $F^{-s} \subseteq G^{-s}$
- F is at least as good for s as G iff:
 - F has at least all pro s factors that G has, and
 - F has at most all con s factors that G has
 - Con s = pro -s



Result model with factors

- Deciding fact situation F for s is **forced** iff there exists a precedent (G, s) such that $G \leq_s F$
 - Such that F is at least as good for s as G
- Deciding F for s is **allowed** iff deciding F for $-s$ is not forced.



$X \leq_s Y$ iff $X^s \subseteq Y^s$ and $Y^{-s} \subseteq X^{-s}$
Deciding F for s is **forced** iff there exists a
precedent (X, Y, s) such that $X \cup Y \leq_s F$

■ *Case 1* – won by **plaintiff**

$\{\pi 1, \pi 3, \delta 1, \delta 3\} \leq_{\pi} \text{FS1?}$

- Deceive-plaintiff ($\pi 1$)
- Security measures ($\pi 3$)
- No-unique-product ($\delta 1$)
- Secrets-disclosed-outsiders ($\delta 3$)

■ *Case 2* – won by **defendant**

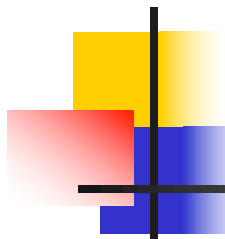
$\{\pi 2, \delta 1, \delta 3\} \leq_{\delta} \text{FS1?}$

- Bribe-Employee ($\pi 2$)
- No-unique-product ($\delta 1$)
- Secrets-disclosed-outsiders ($\delta 3$)

■ *FS 1* –

$\{\pi 2, \pi 3, \delta 2, \delta 3\}$

- Bribe-Employee ($\pi 2$)
- Security measures ($\pi 3$)
- Info-Reverse-Engineerable ($\delta 2$)
- Secrets-disclosed-outsiders ($\delta 3$)



$X \leq_s Y$ iff $X^s \subseteq Y^s$ and $Y^{-s} \subseteq X^{-s}$
Deciding F for s is **forced** iff there exists a
precedent (X, Y, s) such that $X \cup Y \leq_s F$

- *Case 1* – won by **plaintiff**
 - **Deceive-plaintiff** ($\pi 1$)
 - Security measures ($\pi 3$)
 - No-unique-product ($\delta 1$)
 - Secrets-disclosed-outsiders ($\delta 3$)

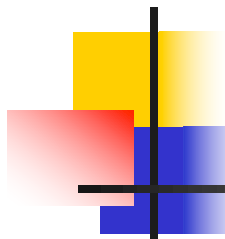
$\{\pi 1, \pi 3, \delta 1, \delta 3\} \leq_\pi \text{FS1? No}$

- *Case 2* – won by **defendant**
 - Bribe-Employee ($\pi 2$)
 - No-unique-product ($\delta 1$)
 - Secrets-disclosed-outsiders ($\delta 3$)

$\{\pi 2, \delta 1, \delta 3\} \leq_\delta \text{FS1?}$

- *FS 1* –
 - Bribe-Employee ($\pi 2$)
 - Security measures ($\pi 3$)
 - **Info-Reverse-Engineerable** ($\delta 2$)
 - Secrets-disclosed-outsiders ($\delta 3$)

$\{\pi 2, \pi 3, \delta 2, \delta 3\}$



$X \leq_s Y$ iff $X^s \subseteq Y^s$ and $Y^{-s} \subseteq X^{-s}$
Deciding F for s is **forced** iff there exists a
precedent (X, Y, s) such that $X \cup Y \leq_s F$

■ *Case 1* – won by **plaintiff**

$\{\pi 1, \pi 3, \delta 1, \delta 3\} \leq_{\pi} \text{FS1?}$

- Deceive-plaintiff ($\pi 1$)
- Security measures ($\pi 3$)
- No-unique-product ($\delta 1$)
- Secrets-disclosed-outsiders ($\delta 3$)

■ *Case 2* – won by **defendant**

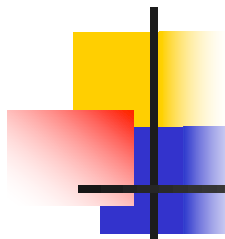
$\{\pi 2, \delta 1, \delta 3\} \leq_{\delta} \text{FS1?}$

- Bribe-Employee ($\pi 2$)
- No-unique-product ($\delta 1$)
- Secrets-disclosed-outsiders ($\delta 3$)

■ *FS 1* –

$\{\pi 2, \pi 3, \delta 2, \delta 3\}$

- Bribe-Employee ($\pi 2$)
- Security measures ($\pi 3$)
- Info-Reverse-Engineerable ($\delta 2$)
- Secrets-disclosed-outsiders ($\delta 3$)



$X \leq_s Y$ iff $X^s \subseteq Y^s$ and $Y^{-s} \subseteq X^{-s}$
Deciding F for s is **forced** iff there exists a
precedent (X, Y, s) such that $X \cup Y \leq_s F$

■ *Case 1* – won by **plaintiff**

$\{\pi 1, \pi 3, \delta 1, \delta 3\} \leq_{\pi} \text{FS1?}$

- Deceive-plaintiff ($\pi 1$)
- Security measures ($\pi 3$)
- No-unique-product ($\delta 1$)
- Secrets-disclosed-outsiders ($\delta 3$)

■ *Case 2* – won by **defendant**

$\{\pi 2, \delta 1, \delta 3\} \leq_{\delta} \text{FS1? No}$

- Bribe-Employee ($\pi 2$)
- **No-unique-product ($\delta 1$)**
- Secrets-disclosed-outsiders ($\delta 3$)

■ *FS 1* –

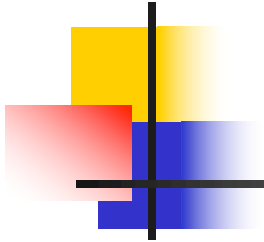
$\{\pi 2, \pi 3, \delta 2, \delta 3\}$

- Bribe-Employee ($\pi 2$)
- **Security measures ($\pi 3$)**
- Info-Reverse-Engineerable ($\delta 2$)
- Secrets-disclosed-outsiders ($\delta 3$)



- plaintiff ← → defendant

0 1 2 3 4 5,

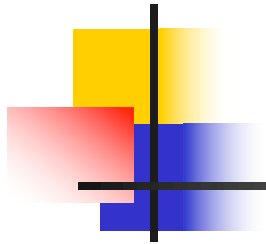


Example dimensions in HYPO

- **Security measures** (minimal measures, access to premises controlled, entry by visitors restricted, entry by employees restricted)

defendant ←———— —————→ plaintiff

minimal < access controlled < entry visitors restr < entry employees restr



Result model with dimensions

- For any two fact situations F and G given a set of dimensions:
 - $G \leq_s F$ iff F is for every dimension at least good for s as G .
- Deciding fact situation F for s is **forced** iff there exists a precedent with fact situation G and decided for s such that $G \leq_s F$

Example (result model for dimensions)

■ Case 1 – won by plaintiff

- d1: Deceive-plaintiff = yes
- d2: Bribe-Employee = no
- d3: Security measures = Entry-By-Visitors-Restricted
- d4: Unique-product = no
- d5: Info-Reverse-Engineerable = no
- d6: Secrets-disclosed-outsiders = 20

■ Case 2 –

- d1: Deceive-plaintiff = no
- d2: Bribe-Employee = yes
- d3: Security measures = Minimal
- d4: Unique-product = no
- d5: Info-Reverse-Engineerable = yes
- d6: Secrets-disclosed-outsiders = 0

d1: Deceive-plaintiff = {no $<_{\pi}$ yes}
d2: Bribe-Employee = {no $<_{\pi}$ yes}
d3: Security-Measures = {Minimal-Measures $<_{\pi}$
Access-To-Premises-Controlled $<_{\pi}$
Entry-By-Visitors-Restricted $<_{\pi}$
Restrictions-On-Entry-By-Employees}
d4: Unique-product = {yes $<_{\delta}$ no}
d5: Info-Reverse-Engineerable = {no $<_{\delta}$ yes}
d6: Secret-disclosed-outsiders = {0 $<_{\delta}$ 1 $<_{\delta}$ 2 $<_{\delta}$...}

Is Case 2 forced for plaintiff?

Example (result model for dimensions)

■ Case 1 – won by plaintiff

- d1: Deceive-plaintiff = yes
- d2: Bribe-Employee = no
- d3: Security measures = Entry-By-Visitors-Restricted
- d4: Unique-product = no
- d5: Info-Reverse-Engineerable = no
- d6: Secrets-disclosed-outsiders = 20

■ Case 2 –

- d1: Deceive-plaintiff = no
- d2: Bribe-Employee = yes
- d3: Security measures = Minimal
- d4: Unique-product = no
- d5: Info-Reverse-Engineerable = yes
- d6: Secrets-disclosed-outsiders = 0

d1: Deceive-plaintiff = {no $<_{\pi}$ yes}
d2: Bribe-Employee = {no $<_{\pi}$ yes}
d3: Security-Measures = {Minimal-Measures $<_{\pi}$
Access-To-Premises-Controlled $<_{\pi}$
Entry-By-Visitors-Restricted $<_{\pi}$
Restrictions-On-Entry-By-Employees}
d4: Unique-product = {yes $<_{\delta}$ no}
d5: Info-Reverse-Engineerable = {no $<_{\delta}$ yes}
d6: Secret-disclosed-outsiders = {0 $<_{\delta}$ 1 $<_{\delta}$ 2 $<_{\delta}$...}

Is Case 2 forced for plaintiff? No.

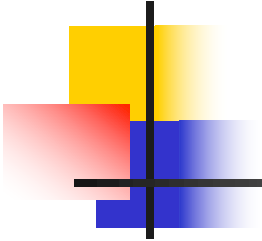


Rosa Ratsma

'Explaining' ML predictions with CBR

- Regard training data as cases/precedents
 - Direction of factors/dimensions can be learned from the BB
- Use AI & law model of CBR for explaining a prediction of the BB model
 - If a precedent **forces** the prediction, then show it
 - Otherwise **explain away** the relevant differences

- H. Prakken & R. Ratsma, A top-level model of case-based argumentation for explanation: formalisation and experiments. *Argument and Computation* 13 (2022): 159-194
- W. van Woerkom et al. A Fortiori case-based reasoning: from theory to data. *JAIR* 81 (2024): 401-441.
- J. Peters et al., Model- and data-agnostic justifications with a fortiori case-based argumentation. *Proceedings of ICAIL 2025*, pp. 102-111.



Example (churning)

- *John will stay with us, since like Maria he recently visited our website. (**citation**)*
- *But Maria also downloaded software from our site while John didn't (**missing pro**). Moreover, John did not reply to our last mailing (**new con**)*
- *But John downloaded a brochure, so like Maria he showed an interest in our products (**substitution**). Moreover, John contacted our help desk, so like Maria he remained in contact with us (**cancellation**)*

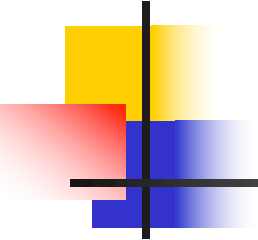


Follow-up work on precedential constraint

Wijnand van Woerkom

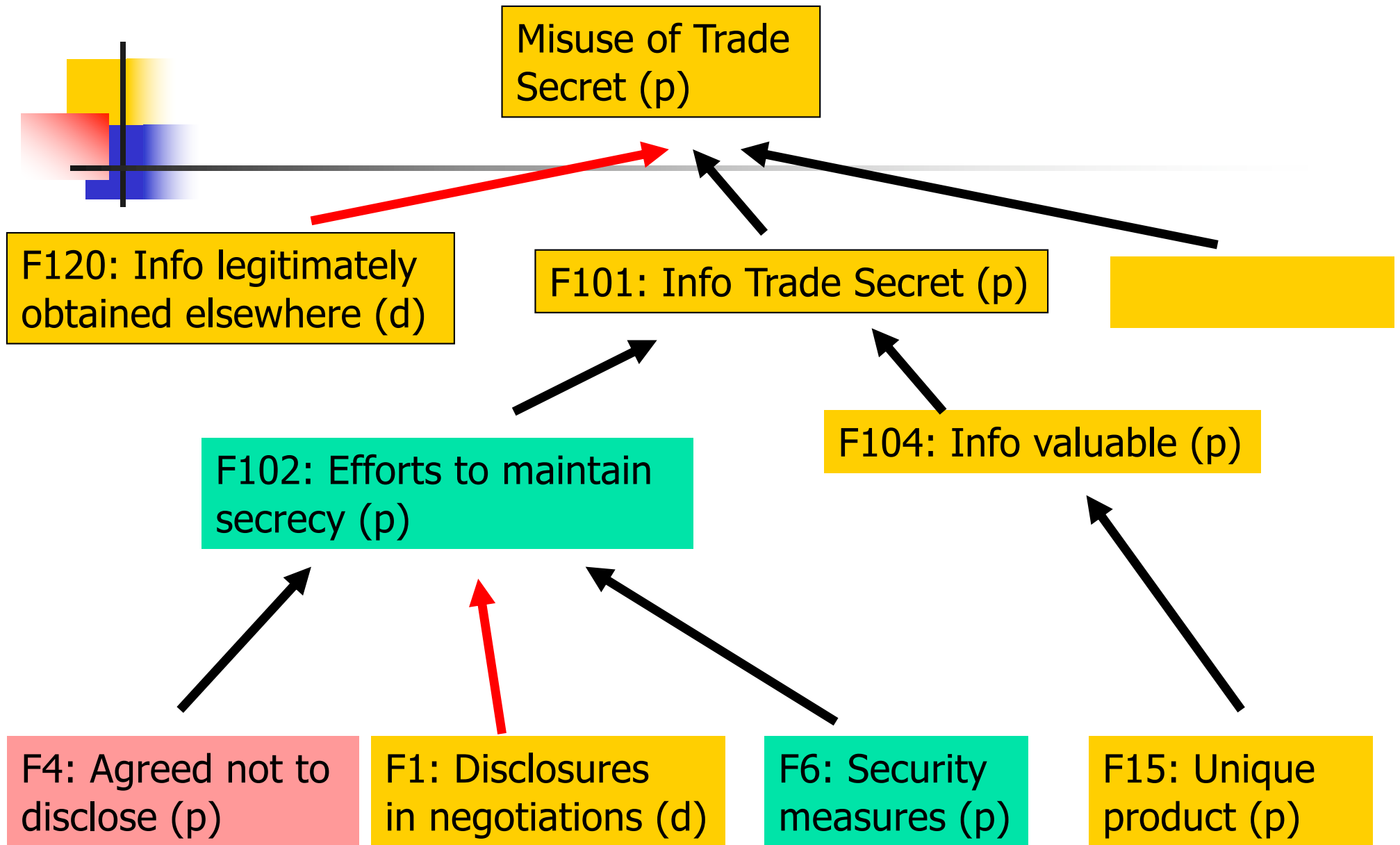
- Discovering dimension orderings in datasets
- **Intermediate** factors in **result** model of precedential constraint
 - Assuming a CATO-style factor hierarchy
 - Generalising it to dimensions
- Implementations with SAT solver

- W. van Woerkom et al. A Fortiori Case-Based Reasoning: From Theory to Data. *JAIR* 81 (2024): 401-441.
- W. van Woerkom et al., Hierarchical models of precedential constraint. *Artificial Intelligence and Law*, in press.



Hierarchical precedential constraint

- Apply precedential constraint to
 - decide on intermediate factors
 - decide on the final outcome given intermediate factors
 - With dimensions: allowed or forced **ranges** of values

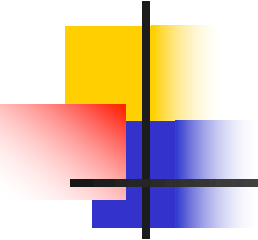




Consistency of datasets

- A case base is **inconsistent** iff it forces opposite outcomes for the same fact situation
- **Degree** of consistency of a CB:
 - The rate of pairs $(F,s), (G,-s)$ for which $F \leq_s G$
- **Authoritativeness** of a case (F,s) : the proportion of cases (G,s) and $(G',-s)$ such that $F \leq_s G$ and $F \leq_s G'$

- R. Ratsma (2020), *Unboxing the Black Box using Case-based Argumentation*. AI Msc thesis, Utrecht University
- J. Peters et al., Justifications derived from inconsistent case bases using authoritativeness. *Proceedings of ArgXAI 2022*.
- W. van Woerkom, Formal results on case-base consistency: a COMPAS case study. *Proceedings of ICAIL*



Decision support for deciding on fitness to drive

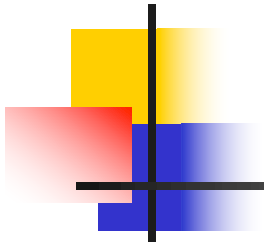
- At Dutch Central Driving License Office
 - “No machine learning”
 - Not transparent or explainable
 - “Is standard CBR useful?”
- Standard CBR:
 - assumes ‘features’ without preferences for decisions
 - applies numerical similarity measures
 - suggests decision of precedent(s) with highest similarity to current case



Joep Nouwens:

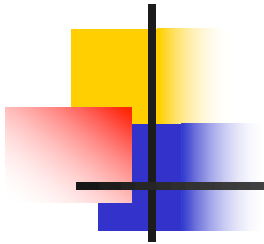
Msc project AI-UU

- Combine and compare with AI & law style CBR:
 - Features with preferences for decisions
 - Not all differences are relevant!
 - Decision-making by precedential constraint
- Example dimensions
 - Heart disease?
 - Bipolar disorder?
 - Eye sight
 - Epilptic attacks
 - ...



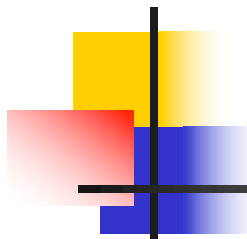
Experiment

- Case base: 15.843 cases, 123 dimensions
 - 80% used as precedent
 - 20% used as test case
- Four decision rules:
 - **Standard CBR**: predict decision with highest similarity
 - **Precedential constraint** with if both allowed/forced:
 - predict 'fit'
 - predict 'unfit'
 - predict decision of case with highest similarity according to standard CBR



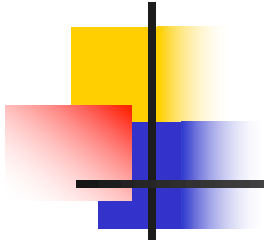
Experiments with accuracies

- Case base: 15.843 cases, 123 dimensions
 - 80% used as precedent
 - 20% used as test case
- Four decision rules:
 - **Standard CBR**: predict decision with highest similarity (92%)
 - **Precedential constraint** with if both allowed/forced:
 - predict 'fit' (70%)
 - predict 'unfit' (64%)
 - predict decision of case with highest similarity according to standard CBR (91%)



The value of predictive experiments

- “High predictive accuracy is evidence of legal correctness of the model”
 - Aleven, Ashley
- HP: only true if system and humans:
 - apply the same knowledge
 - reason with it in the same way



Conclusions

- There is interesting work on symbolic models of legal case-based reasoning
- With recent research applications in
 - Explainable AI
 - Analysing consistency of decision-making
- Initial work on letting LLMs
 - provide the inputs of symbolic models
 - generate case-based arguments
 - (Ashley & students since 2023)