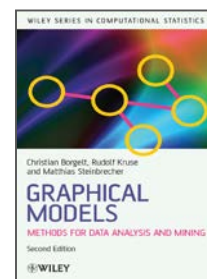
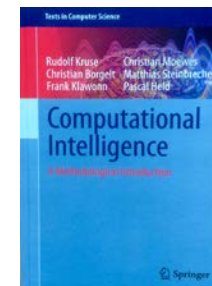
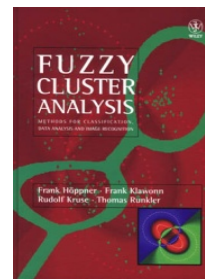
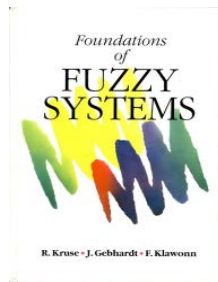
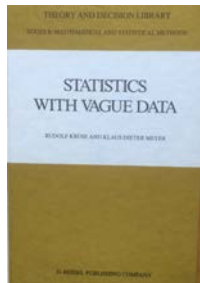


Probabilistic Graphical Models: On Reasoning, Learning, and Revision

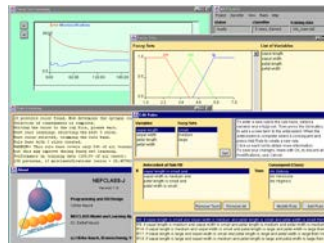
Prof. Dr. Rudolf Kruse

Computational Intelligence Group Magdeburg

Research: Data Sciences, Intelligent Systems www.computational-intelligence.eu



Software Tools: NEFCLASS, Information Miner



Transfers: Industrial Projects (BT, SAP, Siemens, [Volkswagen](#),...), Spin Offs

Property planning - Volkswagen

Property family	Car body	Motor	Radio	Doors	Seat cover	Makeup mirror	...
Property	Hatch-back	2.8 L 150 kW Otto	Type alpha	4	Leather, Type L3	yes	...

Complexity

- About 200 variables
- Typically 4 to 8, but up to 150 possible instances per variable
- More than 2^{200} possible combinations available



Knowledge about the Planning

Rules

- 10000 Technical Rules for Item Combinations, e.g.

IF Motor = m_4 AND Heating = h_1

THEN Generator $\in \{g_3, g_4, g_5\}$

- Often 6-dimensional, sometimes more than 10 dimensions
- 500000 marketing oriented rules (with uncertainty)
- The rules are often changing

Data

- Specification of millions of built cars

Planning Tasks

Calculation of part demands

Compute the installation rate of a given item combination

Simulation

Analyze customers' preferences with respect to those persons who use a navigation system in a VW Polo

Marketing and Sales stipulation

Installation rate of Navigation system increase from 20% to 30%

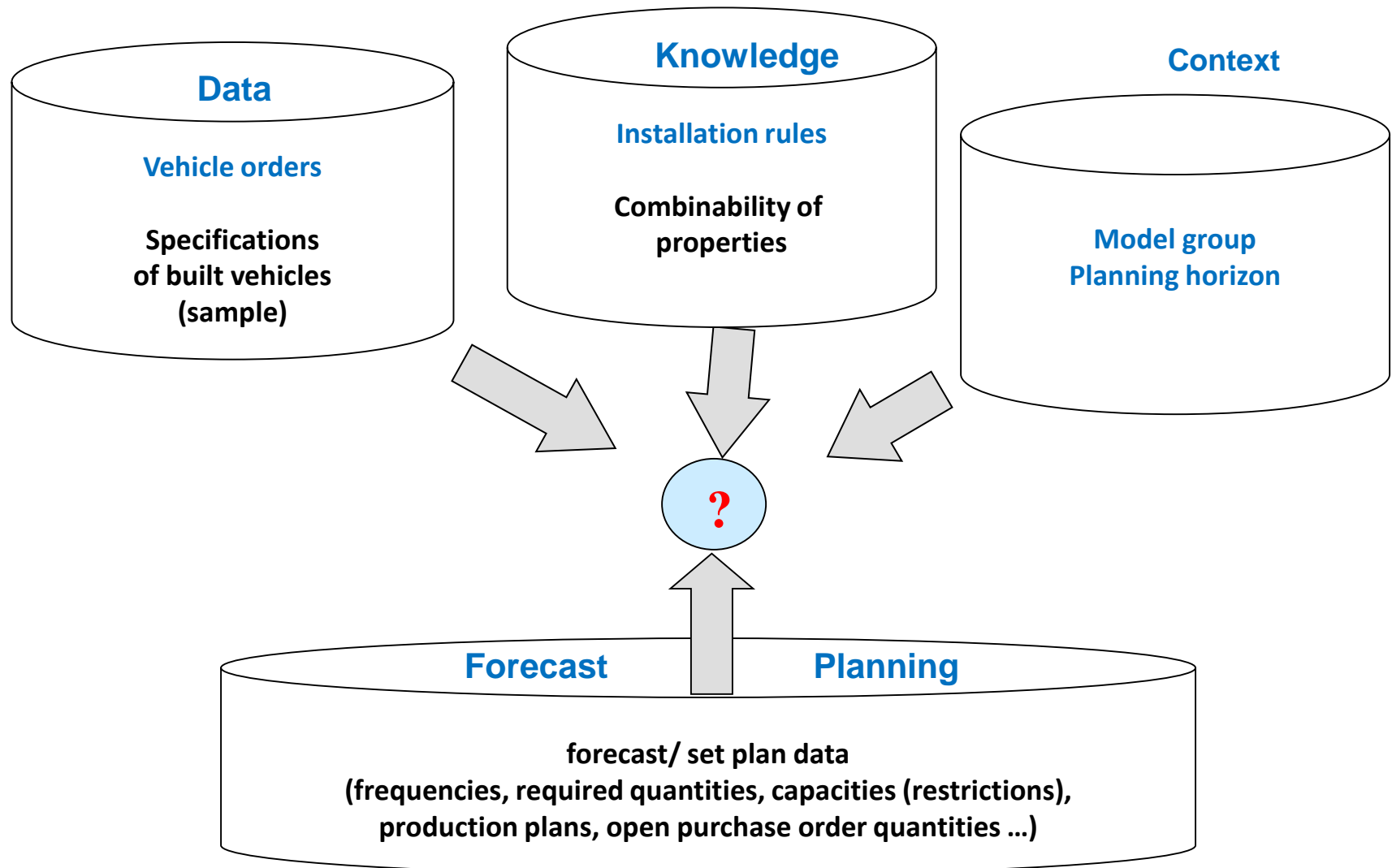
Capacity Restrictions

Maximum availability of seat coverings in leather is 5000

Belief Change (EC Project Defeasible Reasoning)

Gärdenfors: An agent (planner) is in a Belief State,
he is using the operations **Focussing** and **Revision**

How to manage the **uncertain** information about planning?



Requirements for the Planning System

- Assistant System for Handling Estimates for Installation Rates
- **The planners should enjoy comfort without losing competence**
- Explanation of the Results (Explainable AI)
- Explicit, Sound, Transparent Model
- Answers to the planners questions in real time (seconds)
- Different Model Groups and Different Planning Intervals:
5000 planning scenarios handled by 350 planners worldwide
- Implementation by a CI Group spin off (lead by Jörg Gebhardt)

Our Modelling Approach: Decomposable Models

Configuration Management: Relations

Installation Rate Management: Subjective Probabilities

Problem

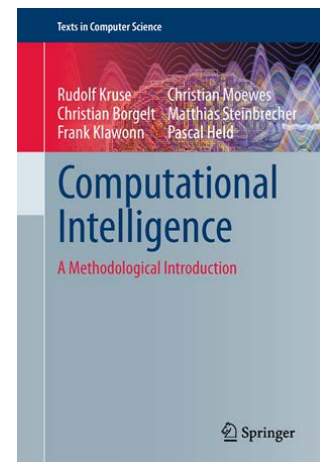
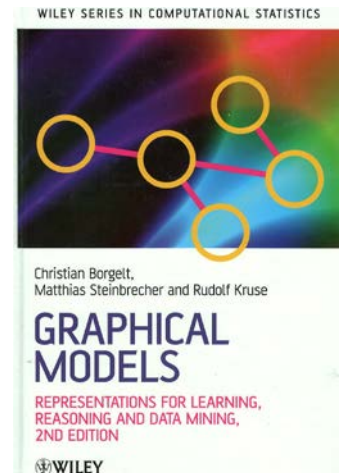
High dimensionality (here typically 200 dim)

Solution: Decomposition

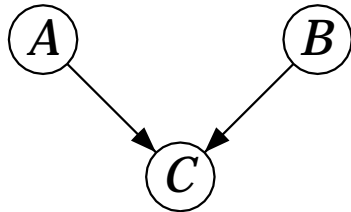
Instead of one high dimensional global model use
several connected local low dimensional models

Graphical Models

Relational, Possibilistic, Bayes- and Markov-Networks



How to find a suitable **decomposition** of a probability space?



A,B,C (Random) Variables

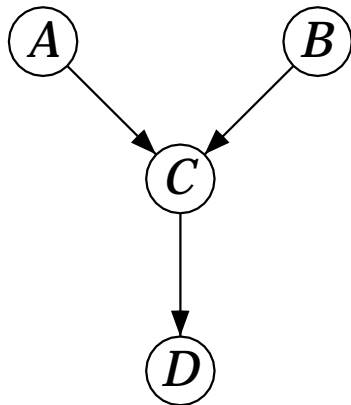
A quality of ingredients

B cook's skill

C meal quality

If C is not known, A and B are independent.

If C is known, then A and B become (conditionally) dependent given C.



A,B,C,D (Random) Variables

A quality of ingredients

B cook's skill

C meal quality

D restaurant success

If nothing is known about the restaurant success or meal quality or both, the cook's skills and quality of the ingredients are unrelated, that is, independent.

However, if we observe that the restaurant has no success, we can infer that the meal quality might be bad.

If we further learn that the ingredients quality is high, we will conclude that the cook's skills must be low, thus rendering both variables dependent.

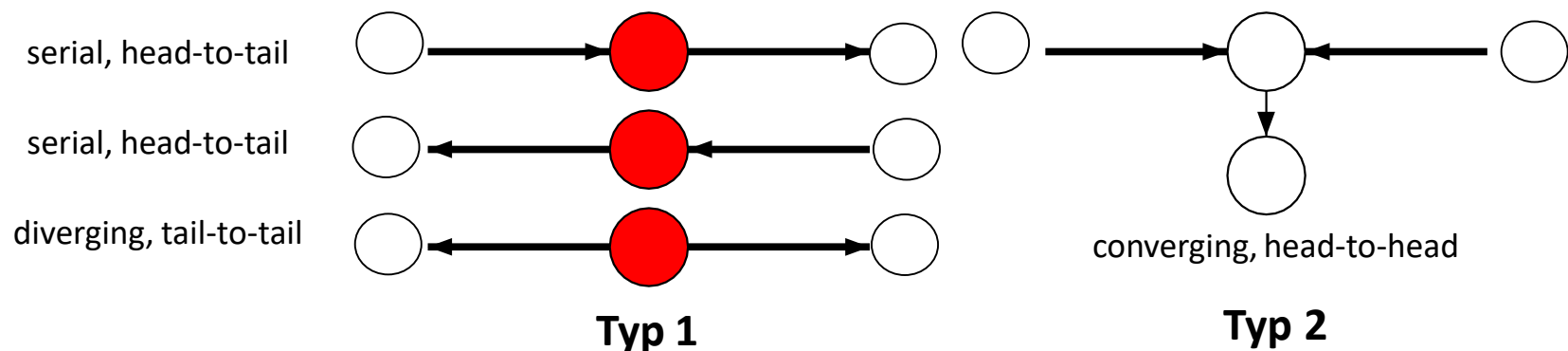
Decomposition: $P(A,B,C,D) = P(A)P(B)P(C|A,B)P(D|C)$

Separation in directed Graphs (d-separation)

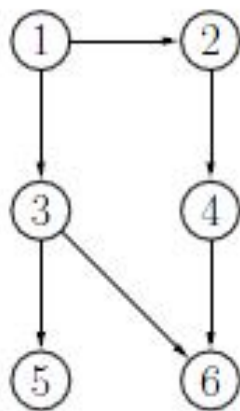
Z d-separates X from Y if all paths (paths in reverse to arrows are allowed) from X to Y are blocked by a node in Z .

A node A is blocking a path, if its edge directions along the path

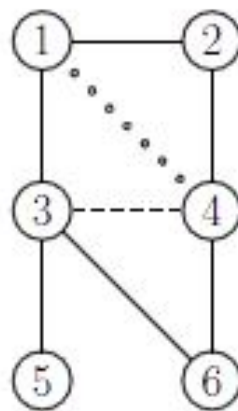
- are of type 1 and $A \in Z$, or
- are of type 2 und neither A nor one of its descendants is in Z .



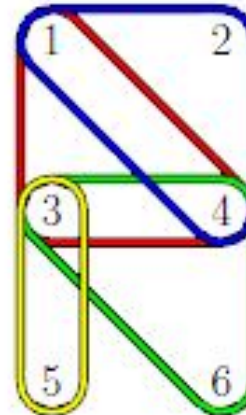
Decomposition: Automatic Join Tree Generation using d-separation



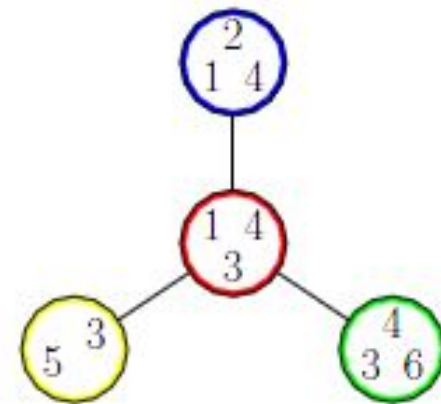
original
graph



triangulated
moral graph



maximal
cliques



join tree

Efficient Reasoning in Markov-Networks

Consistent Decomposition

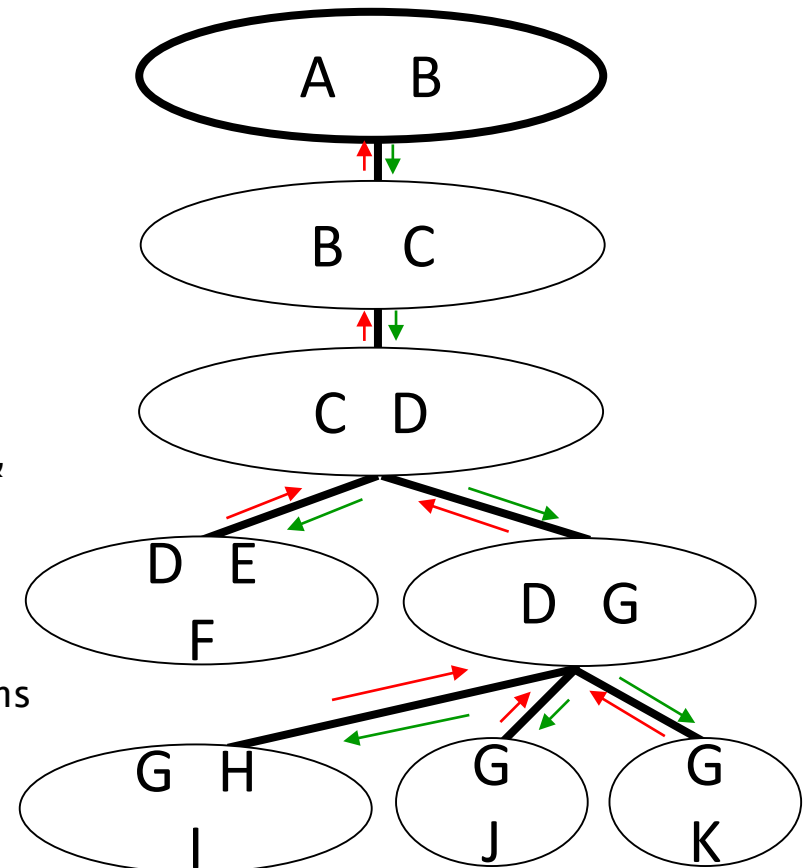
- Distributions only over the cliques (conditional independencies)
- Validity of all combinations registered and available

Fast Conditioning in Hyper Tree

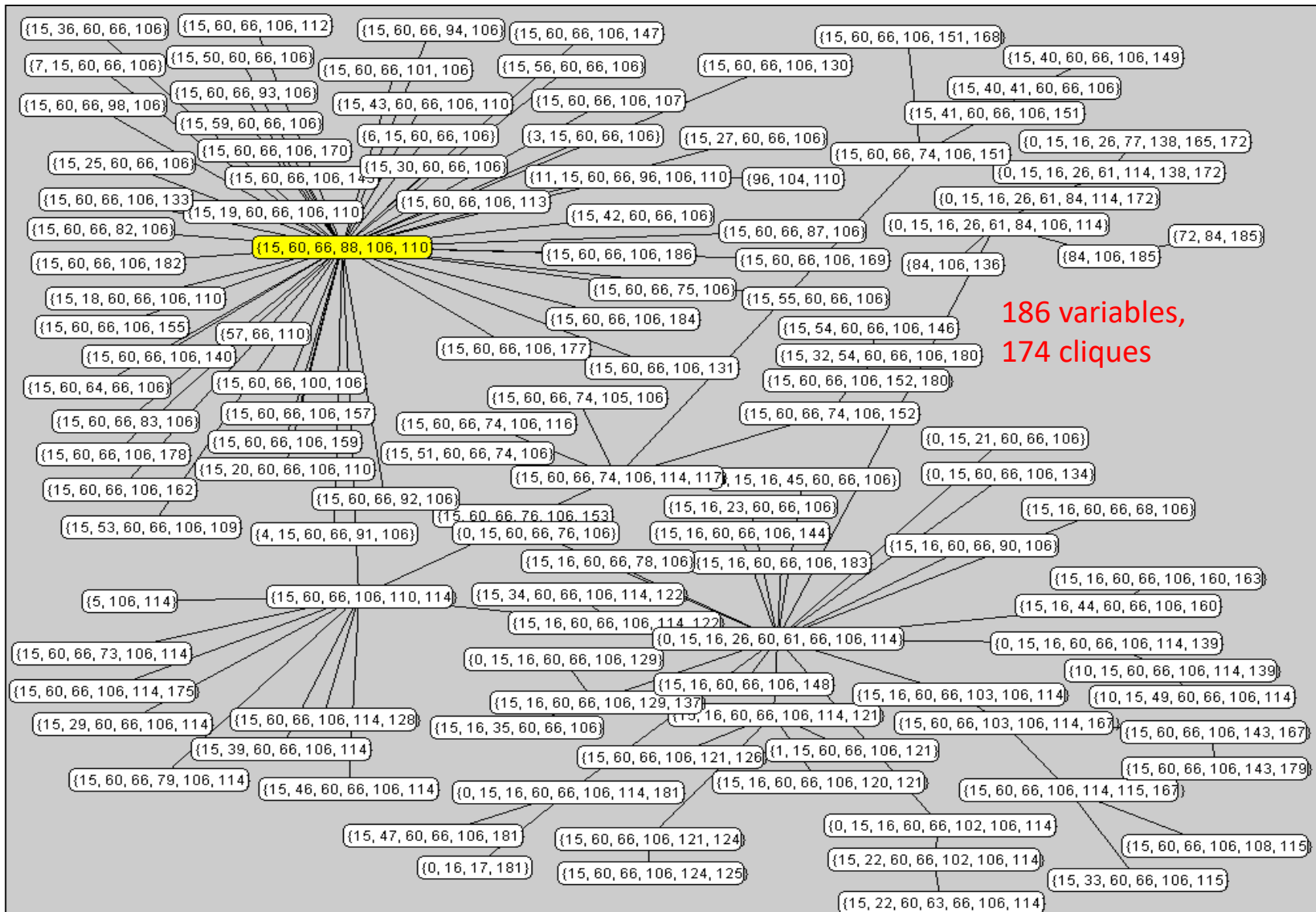
- Propagation by traversing the net twice (collect & distribute)

Efficient planning

- Planning requirements as conditional distributions
- Calculation of frequencies for arbitrary property combinations (focusing analyses, simulations) in real time



Example: Markov Network for VW Bora



Example: System EPL (EigenschaftsPLanung) at VW

In worldwide use : 15 developers, 350 planners

Different planning responsibilities with individual workflow

- Structure Induction
- Base distribution
- Assessment of demand for approx. 40 planning intervals (weeks, months)
- 5000 different Markov networks in use daily
- Focusing: Fast calculation of conditional and marginal probabilities

Example for one planning week

Data volume (cumulative per week)	Across all 166 Model groups	Single Model group
Number of Markov Nets	75.787	1.054
Total size (compressed)	79,9 GB	3,8 GB
... for one planning interval	Model group 1	Model group 2
Planning requirement	4.424	1.299
Number of variables	203	204
Number of cliques	174	156
Network size (compressed, RAM: ~Factor 10)	8,5 MB	17,9 MB
Largest clique (only positive probabilities)	130.806 tuples 9 variables	1.489.515 tuples 14 variables

Relevant research topics

Fusion of Qualitative and Quantitative Knowledge

Data, Rule Systems, Conditional Independence Statements, Contexts

Learning the Model from Data

Local and Global Structure

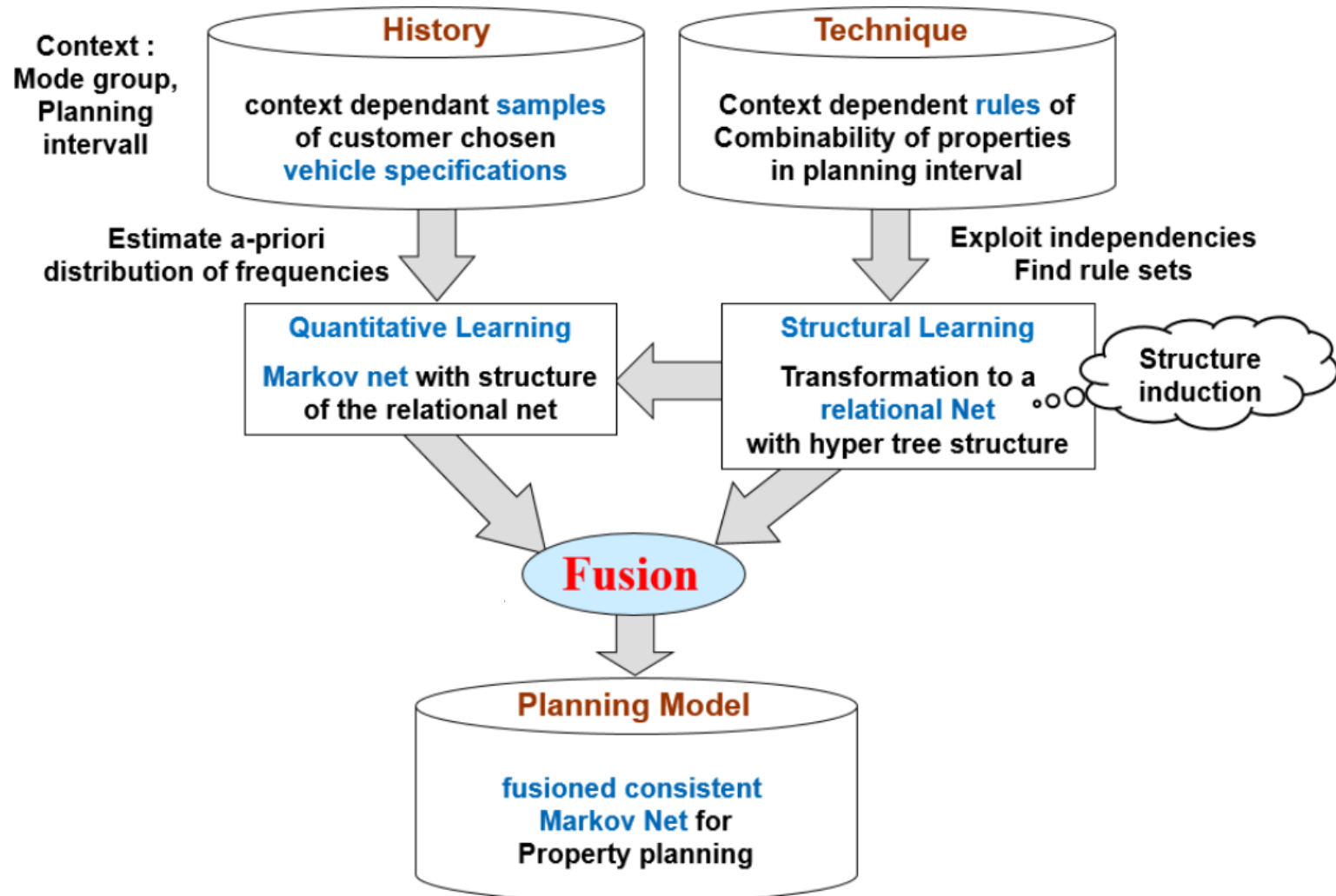
Revision of Big Decomposable Models

Relational, Probabilistic Graphical Models

User Interaction

Handling Inconsistencies, Explanation of Solutions, Level of Assistency

How to learn new Planning Models?



Revision

Prior Probability
Distribution

New Conditional Probabilities:
Marketing Stipulations, Capacity Restrictions



REVISION

Principle of minimal Change



Posterior Probability Distribution including
specified and inferred changes.

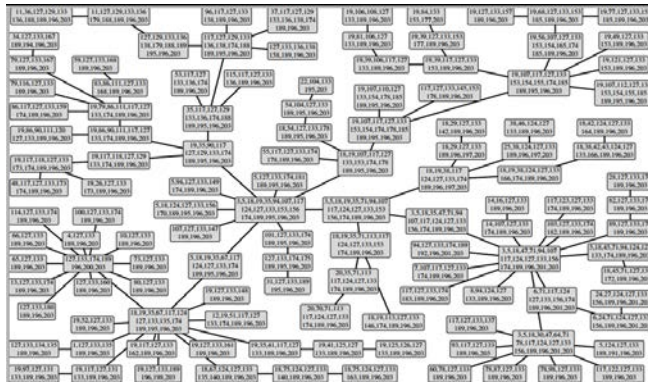
Information-theoretically closest to the
prior distribution

Revision Operator

- Iterative Proportional Fitting (Biproportional Fitting, RAS Algorithm, Matrix Scaling)
- Algorithms for Adapting the Marginal Distributions
- Stepwise Modification of the Probability Distribution
- Process converge for Non-Contradicting Revision Statements
- Approx. 7000 Revision Assignments per Week and Model

Inconsistencies

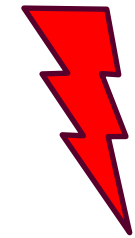
Complex Structure



Many Changes

Inconsistencies

1450	51	27	30	000001	POCHI
1450	51	27	30	000002	POCHI
1450	51	27	30	000003	POCHI
1450	51	27	30	000004	POCHI
1450	51	27	30	000005	POCHI
1450	51	27	30	000006	POCHI
1450	51	27	30	000007	POCHI
1450	51	27	30	000008	POCHI
1450	51	27	30	000009	POCHI
1450	51	27	30	000010	POCHI
1450	51	27	30	000011	POCHI
1450	51	27	30	000012	POCHI
1450	51	27	30	000013	POCHI
1450	51	27	30	000014	POCHI
1450	51	27	30	000015	POCHI
1450	51	27	30	000016	POCHI
1450	51	27	30	000017	POCHI
1450	51	27	30	000018	POCHI
1450	51	27	30	000019	POCHI
1450	51	27	30	000020	POCHI
1450	51	27	30	000021	POCHI
1450	51	27	30	000022	POCHI
1450	51	27	30	000023	POCHI
1450	51	27	30	000024	POCHI
1450	51	27	30	000025	POCHI
1450	51	27	30	000026	POCHI
1450	51	27	30	000027	POCHI
1450	51	27	30	000028	POCHI
1450	51	27	30	000029	POCHI
1450	51	27	30	000030	POCHI
1450	51	27	30	000031	POCHI
1450	51	27	30	000032	POCHI
1450	51	27	30	000033	POCHI
1450	51	27	30	000034	POCHI
1450	51	27	30	000035	POCHI
1450	51	27	30	000036	POCHI
1450	51	27	30	000037	POCHI
1450	51	27	30	000038	POCHI
1450	51	27	30	000039	POCHI
1450	51	27	30	000040	POCHI
1450	51	27	30	000041	POCHI
1450	51	27	30	000042	POCHI
1450	51	27	30	000043	POCHI
1450	51	27	30	000044	POCHI
1450	51	27	30	000045	POCHI
1450	51	27	30	000046	POCHI
1450	51	27	30	000047	POCHI
1450	51	27	30	000048	POCHI
1450	51	27	30	000049	POCHI
1450	51	27	30	000050	POCHI
1450	51	27	30	000051	POCHI
1450	51	27	30	000052	POCHI
1450	51	27	30	000053	POCHI
1450	51	27	30	000054	POCHI



Outer Inconsistencies

Revision assignments inconsistent with zero-values in prior distribution

Inner Inconsistencies

Revision assignments are inconsistent, independent of prior distribution

Inconsistencies: Examples

	0,6	0,3	
	0,2	0,25	
0,5	0,3		
			0,1

	0,6	0,3	0,1
	0,2	0,25	0,0
0,5	0,3		0,0
	0,1		0,1

$(0,2 + 0,25 = 0,45)$
 $(1 - 0,5 - 0,45 = 0,05)$

Conflict!!!

Inner Inconsistency

	0,1	0,5	0,4
0,3		●	●
0,5		●	

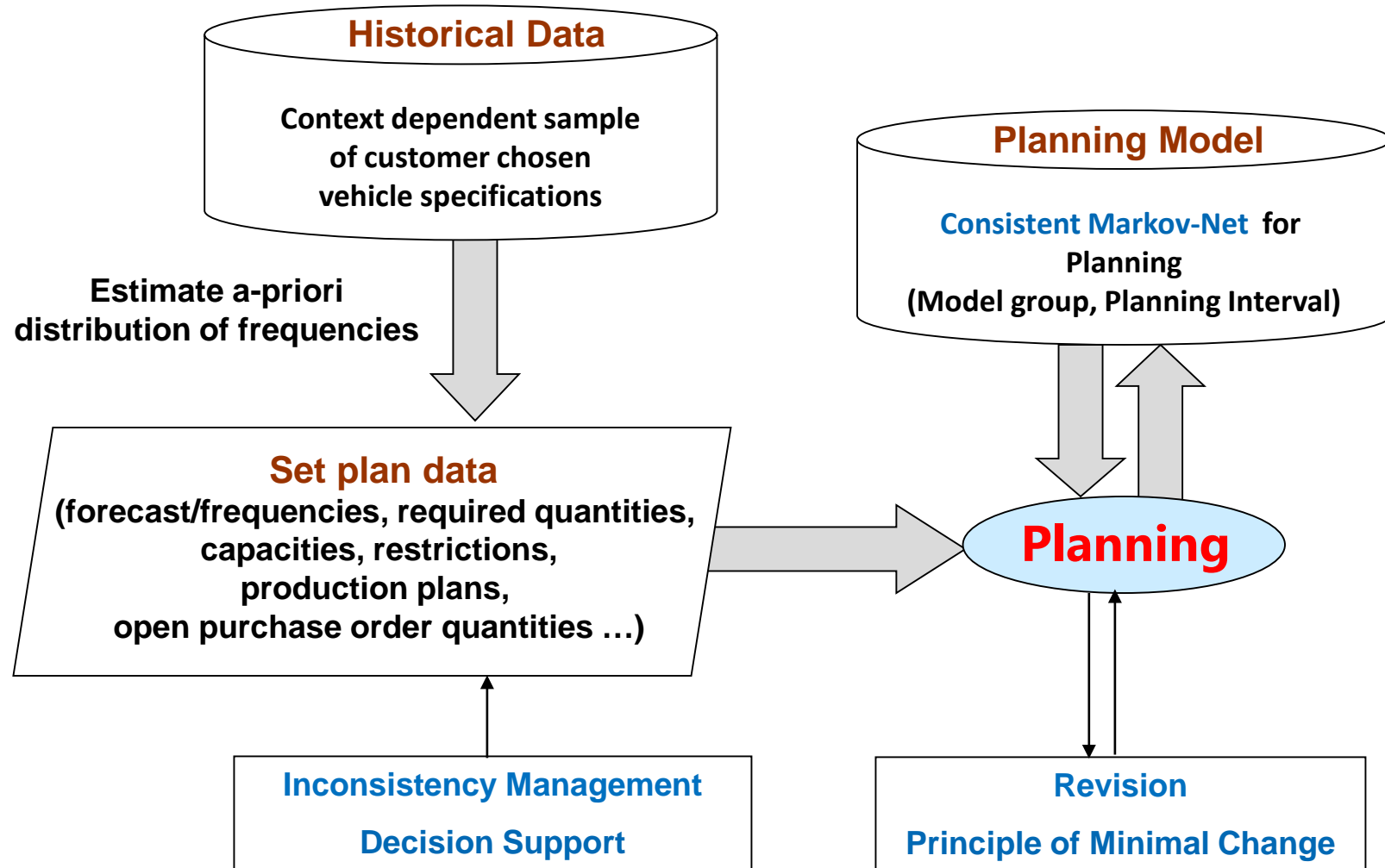
	0,1	0,5	0,4
0,3		●	●
0,5		●	
0,2		0,5	

Conflict!!! $0,3 + 0,5 + 0,5 > 1!$

Outer Inconsistency

It is not easy to configure revision statements without creating inconsistencies!
How to explain the user how to change his desired revision statements?

Planning Operation: Revision



Conclusion

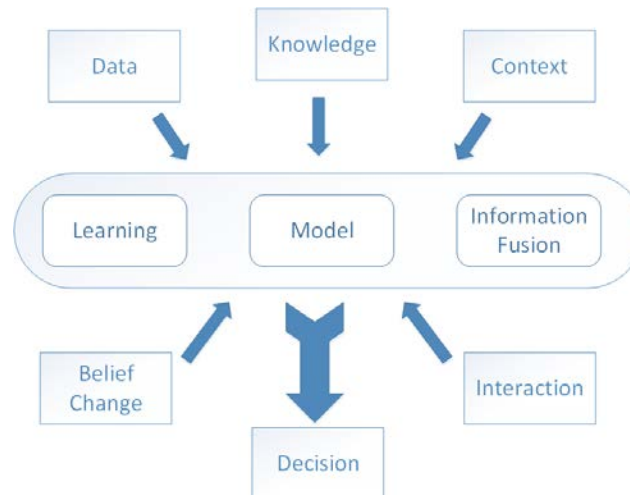
For assistant systems in industry pure data driven approaches are often not sufficient due to deficits in explainability.

The combination of quantitative (data, learning) and qualitative (knowledge about independence, causalities, rules, contexts) methods often gives more powerful frameworks for solving high-dimensional problems.

Current methods of computational intelligence can handle hundreds of variables, high-dimensional dependencies, and context information, while the human expert steers the process and validates the results.

Conclusion

The methodology in this application can be transferred to other areas



Lots of interesting technical problems:

How to ensure reliability in autonomous system (e.g. cars):?

How to explain the results to the user?

Don't forget:

The human should be in the centre of AI solutions – social and legal aspects are often more important for success than technical aspects

What comes next in AI?

BBVA Foundation

Frontiers of Knowledge Awards 2022

Category: Information and Communication

Winner:

Judea Pearl



What comes next in AI?

Associations (“observing”) Bayes, belief, conditional probability,...

What does a symptom say about a disease? How would observing X change my belief in Y?

Intervention (“doing”) Do-Operator, model revision,...

If I take aspirin, will my headache be cured? What would Y be if I did X?

Causality („understanding“) Counterfactuals,...

Was it X that caused Y? What if X hadn't occurred? What if I had acted differently? Did Aspirin Stop My Headache? What if I hadn't smoked in the last 2 years?